

Preliminary weight estimation

Short summary of all weight estimation formulas:


$$W_{to} = W_{oe} + W_{pl} + W_f$$

W_{to} = takeoff weight
 W_{oe} = operational empty weight
 W_{pl} = payload weight
 W_f = fuel weight


$$\begin{aligned}
 W_{to} &= W_e + W_f + W_{pl}(\text{tot}) + W_{tfo} \\
 &= a \cdot W_{to} + b \quad \quad \quad = W_{pl} + W_{crew} \quad \quad \quad = M_{tfo} \cdot W_{to} \\
 & \quad \quad \quad \downarrow \quad \quad \quad \downarrow \quad \quad \quad \downarrow \\
 & \quad \quad \quad = W_f(\text{res}) + W_f(\text{used}) \\
 & \quad \quad \quad \downarrow \\
 & \quad \quad \quad = M_{res} \cdot W_f(\text{used})
 \end{aligned}$$

W_e = empty weight
 $W_{pl}(\text{tot})$ = total payload weight
 W_{tfo} = trapped fuel weight
 a and b = constant from W_e vs. W_{to} graph
 $W_f(\text{res})$ = reserve fuel weight
 $W_f(\text{used})$ = usable fuel weight
 M_{res} = fraction of mission fuel
 W_{crew} = crew weight
 M_{tfo} = fraction of takeoff weight


Additional equations for range and endurance:




Propeller driven aircraft $R = \left(\frac{\eta_p}{g \cdot c_p} \right)_{\text{cruise}} \cdot \left(\frac{L}{D} \right)_{\text{cruise}} \ln \left(\frac{W_4}{W_5} \right)$



Jet driven aircraft $R = \left(\frac{V}{g \cdot c_j} \right)_{\text{cruise}} \cdot \left(\frac{L}{D} \right)_{\text{cruise}} \ln \left(\frac{W_4}{W_5} \right)$



- Propeller driven aircraft $E = \left(\frac{\eta_p}{V \cdot g \cdot c_p} \right)_{\text{loiter}} \cdot \left(\frac{L}{D} \right)_{\text{loiter}} \ln \left(\frac{W_8}{W_9} \right)$



- Jet driven aircraft $E = \left(\frac{1}{g \cdot c_j} \right)_{\text{loiter}} \cdot \left(\frac{L}{D} \right)_{\text{loiter}} \ln \left(\frac{W_8}{W_9} \right)$

Where:

E = endurance (in sec):

$(L/D)_{\text{loiter}}$ = aerodynamic efficiency for maximum loiter time

Important references from slides:

Class I weight prediction method

$$W_{TO} = W_{OE} + W_F + W_{PL}$$

$$W_{OE} = W_E + W_{tfo} + W_{crew}$$

$$W_{tfo} = M_{tfo} * W_{TO}$$

$$M_{tfo} = 0.001 - 0.005$$

$$W_{PLtot} = W_{PL} + W_{crew}$$

ATT! The payload load can include the crew (the pilot) in case of small utility aircraft

$$W_{TO} = W_E + W_F + W_{PLtot} + M_{tfo} * W_{TO}$$

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Weight data from statistics

$$W_{TO} = W_E + W_F + W_{PLtot} + M_{tfo} * W_{TO}$$

$$W_E = a * W_{TO} + b$$

a and b derived from the linear regression of reference aircraft weight data (W_E and W_{TO})

From the examples of previous slides*:

Single engine prop. aircraft: $a = 0.5482$; $b = 486.68$

Business jet aircraft: $a = 0.5417$; $b = 579.96$

Fuel weight estimation method

$$W_{\text{Fused}} = (1 - M_{\text{ff}}) * W_{\text{TO}}$$

$$M_{\text{ff}} = \frac{W_1}{W_{\text{TO}}} \frac{W_2}{W_1} \frac{W_3}{W_2} \frac{W_4}{W_3} \frac{W_5}{W_4} \frac{W_6}{W_5} \frac{W_7}{W_6} \frac{W_8}{W_7} \frac{W_9}{W_8} \frac{W_{10}}{W_9} \frac{W_{\text{final}}}{W_{10}}$$

