

$$\boxed{2/51} \quad U_p: \quad a_u = -g - kv^2 = v \frac{dv}{dy} \quad \uparrow y$$

$$\int_0^h dy = - \int_{v_0}^0 \frac{v dv}{g + kv^2}$$

$$h = - \frac{1}{2k} \ln [g + kv^2] \Big|_{v_0}^0 = \frac{1}{2k} \ln \left[\frac{g + kv_0^2}{g} \right]$$

$$h = \frac{1}{2(0.002)} \ln \left[\frac{32.2 + 0.002(100)^2}{32.2} \right] = \underline{120.8 \text{ ft}}$$

$$\text{Down:} \quad a_d = -g + kv^2 = v \frac{dv}{dy}$$

$$\int_h^0 dy = \int_0^{v_f} \frac{v dv}{-g + kv^2}$$

$$-h = \frac{1}{2k} \ln [-g + kv^2] \Big|_0^{v_f} = \frac{1}{2k} \ln \left[\frac{g - kv_f^2}{g} \right]$$

$$\Rightarrow v_f = \sqrt{\frac{g}{k} (1 - e^{-2kh})}$$

$$= \sqrt{\frac{32.2}{0.002} (1 - e^{-2(0.002)(120.8)})} = \underline{78.5 \frac{\text{ft}}{\text{sec}}}$$