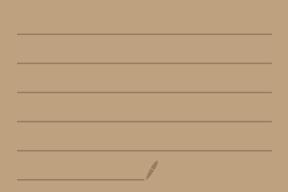
# Propulsion and Power



#### ELEMBUTS OF A PROPULSION SYSTEM

3. thrust producing mechanism

1. Energy source 2. Energy to work converter

1. Juel cells batteries Uydogen basoline

egiles

2. Different 3. Propeller Nozzle

#### THEEMODYNAMICS:

# Footh daw: Thermal equilibrium and the concept of temperature

First daw: Conservation of energy and its interconvertability

- · ΔE = ΔKE + ΔPE + ΔU = constant U= internal → independent of P and V
- · enthalpy: h= n+p·v

- U= PLT) and dU = Cv. dT
- · Cv = (20/2T) v so du = Cv·dT constant volume only
- · Cp = (dh/dT)p so dh = Cp. OT constant pressure only.

Second daw: Defines entropy [ ]/hs k or //k male]

- · measure of randomness and disorder
- · State function
- · Change of entropy  $\Delta S = Sfind Sinital -> negative means more order.$
- · Thereases in a spontaneous proces, dicreases in an equilibrium process.
- · The entropy change in a irreverible process is always positive.

Third daw: Entropy of a system is 0 at absolute 0 K.

# BASIC EQUATIONS FOR IDEAL GAS:

- · Ideal gas if P.V = R.T P= pressure | V = specific volume | R = gas constat | T= abs temperature
- · Went supply at a constant pressure.

  - · (dQ/dT)p = Cu+p·(dV/dT)p
  - · P·V = R·T so p·(dv/oT)p=R
  - · Gp = Cv + R

•  $dh = \partial Q_p = du + p dv = Cv \partial T + p \partial v$  Ratio between Cp/Cv = k isentropic component.

#### Ideal cas daw:

Isothermal process: p.v = constant

· Isobaric process: V/T = constant

· Jsochloric process: P/T = constant

· Jertropic process: p. V = constant

· Polytropic process: p. V = constant

#### JEENTROPIC Process:

$$\cdot RT \cdot V^{k-1} = constant$$
  $R = constant$ 

$$\bullet$$
 T.  $V^{k-1} = constant$ 

• 
$$P \cdot V = R \cdot T \rightarrow V = \frac{RT}{D}$$

• 
$$P \cdot \left(\frac{RT}{P}\right)^n = constant$$

$$P = \frac{(1-h)}{a} \cdot T = constant$$

$$\left(\frac{1}{p}\right)^{\frac{|k-1|}{k}} = constant$$

$$\frac{1}{\sqrt{1}} = \left(\frac{\frac{1}{2}}{\frac{2}{1}}\right)^{\frac{(n-1)}{n}}$$

• 
$$T_2 = T_1 \cdot \prod^{(h-1)/h} = \frac{P_2}{P_1}$$

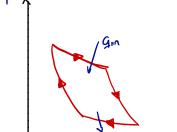
$$T_{2} = \left(\frac{P_{2}}{P_{1}}\right)^{\frac{(k-1)}{k}}$$

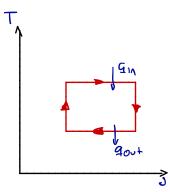
$$T_{2} - T_{1} = T_{1} \cdot \left\{ \prod^{(k-1)/k} - 1 \right\}$$

# POWER CYCLES:

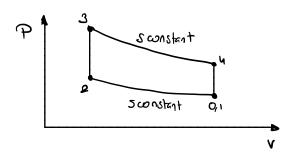
# CARNOT CYCLE: I deal Process.

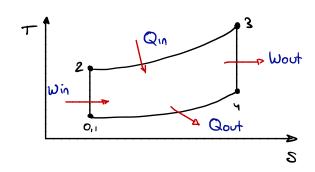
- . Isothermal heat adition and expansion
- · Isentropic expansion
- · Isothermal compressions and heat rejection
- · Isutropic compression





#### SECOND DECTURE Otto Cycle:





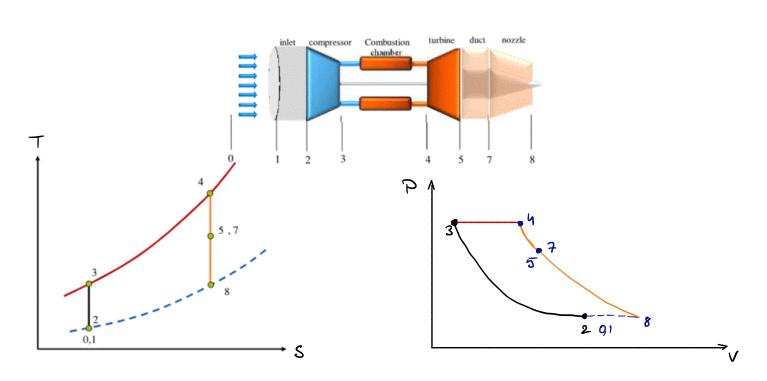
$$\eta_{th} = \frac{W_{net}}{q_{in}}$$

Process 1-2 and 3-4 are isentropic, and  $V_2 = V_3$  and  $V_4 = V_1$ 

$$\frac{\overline{T_1}}{\overline{T_2}} = \left(\frac{\sqrt{2}}{V_1}\right)^{k-1} = \left(\frac{\overline{V_3}}{V_4}\right)^{k-1} = \frac{\overline{T_1}}{\overline{T_3}} \longrightarrow \frac{\overline{T_1}}{\overline{T_n}} = \frac{\overline{T_2}}{\overline{T_3}} \quad \text{So} \quad \boxed{V_{th} = 1 - \frac{1}{T_2}}$$

$$\eta_{th} = 1 - \frac{\uparrow_1}{T_2}$$

$$M_{14} = 1 - \frac{T_1}{T_2} = 1 - \left(\frac{v_2}{v_1}\right)^{n-1} = 1 - \left(\frac{1}{CR}\right)^{n-1}$$
   
 $CR = compression ratio. CR > 1$ 

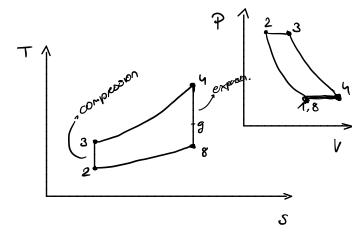


· I deal gas with constant Co and Cu and constant composition.

BRAYTON CYCLE

- · Constant mass flow
- Compression and expansion adiabatic and reversible.
- · No pressure losses
- $^{\bullet}$   $\Delta$  lunetic energy per component = O

IDEAL CYCLE - Process DATA



 $\Pi$  is the pressure ratio of the cycle  $\Pi = P3/pe = Pn/p_{on}$  k = Cp/Cv

nth = Thermal efficiency of the cycle:

$$\operatorname{Dth} = \left( \frac{\operatorname{work \ output}}{\operatorname{heat \ input}} \right) = \left( \frac{\operatorname{Wu-8 - W_{2-3}}}{\operatorname{Q}_{3-4}} \right) = \left( \frac{\operatorname{Cp}(T_1 - T_8) - \operatorname{Cp}(T_3 - T_2)}{\operatorname{Cp}(T_1 - T_3)} \right)$$

$$Nth = \left(\frac{\left(T_4 - T_8\right) - \left(T_3 - T_2\right)}{\left(T_4 - T_3\right)}\right)$$

$$\left(\frac{T_{i}}{T_{g}}\right) = \prod_{i} \frac{k_{-i}}{n}$$
 and  $\frac{1}{T_{2}} = \prod_{i} \frac{k_{-1}}{n}$ 

$$\frac{\overline{13}}{\overline{12}} = \int \frac{h-1}{n}$$

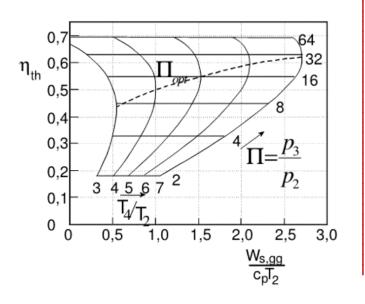
$$\eta_{U_{1}} = \left(\frac{T_{1}\left(1 - \frac{T_{2}}{T_{1}}\right) - T_{3}\left(1 - \frac{T_{2}}{T_{3}}\right)}{\left(T_{1} - T_{3}\right)}\right) = \left(\frac{T_{1}\left(1 - \frac{1}{\prod \frac{n-1}{n}}\right) - T_{3}\left(1 - \frac{1}{\prod \frac{n-1}{n}}\right)}{\left(T_{1} - T_{3}\right)}\right) = \left(\frac{T_{1}\left(1 - \frac{1}{T_{3}}\right)\left(1 - \frac{1}{\prod \frac{n-1}{n}}\right)}{\left(T_{1} - T_{3}\right)}\right)$$

$$P_{3} = P_{4} \left( \frac{T_{5}}{T_{4}} \right)^{\frac{L}{L-1}} = P_{2} \prod_{n} \left[ 1 - \frac{T_{2}}{T_{n}} \left( \prod_{n-1} \frac{L}{L-1} \right) \right]^{\frac{L}{L-1}}$$

# Specific Power:

$$\frac{W_{s,gs}}{C_{p}T_{2}} = \frac{T_{4}}{T_{2}} \left[ 1 - \frac{1}{\prod_{k=1}^{k-1}} \right] - \left[ \prod_{k=1}^{k-1} - 1 \right]$$

# Specific Power and Efficieng:



# Optimal Prossure Ratio

$$W_{SS} = W_{S-8} = M_{Cp} \left( T_{g} - T_{g} \right)$$

$$\prod_{\alpha} \frac{\alpha_{-1}}{\alpha} = \frac{T_{3}}{T_{2}} = \frac{T_{\alpha}}{T_{\delta}} \longrightarrow \boxed{T_{g} = \frac{T_{\alpha}}{T_{3}} T_{2}}$$

Differentiate Was w.r.t To and escuenting to zero

$$\omega_{5\delta} = M C_{\rho} \left( \overline{1}_{5} - \frac{\overline{1}_{4}}{\overline{1}_{3}} \overline{1}_{2} \right) = -M C_{\rho} \bullet \frac{\overline{1}_{4} \cdot \overline{1}_{2}}{\overline{1}_{3}^{2}}$$

$$\overline{1}_{3} = \left( \overline{1}_{2} \cdot \overline{1}_{4} \right)$$

$$\bigcap_{\rho \uparrow} = \left( \frac{\overline{1}_{3}}{\overline{1}_{2}} \right)^{\frac{L}{L-1}} = \left( \frac{\overline{1}_{4}}{\overline{1}_{2}} \right)^{\frac{L}{2(L-1)}}$$

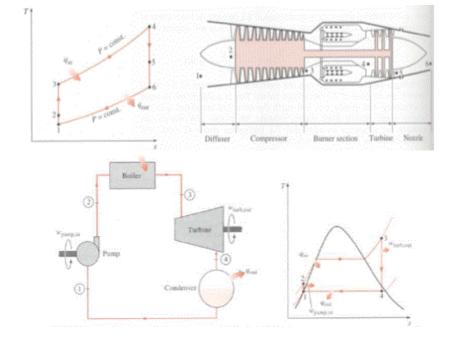
Thus: 
$$\frac{W_{s,gs}}{C\rho T_2} = max$$
 when

$$\left(\frac{\omega_{\delta,5\delta}}{C_{p}T_{2}}\right)_{\text{Nopt}} = \left(\sqrt{\frac{T_{4}}{T_{2}}} - 1\right)^{2}$$

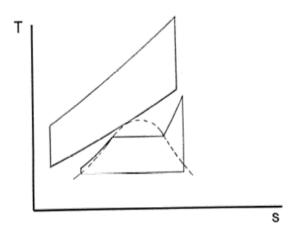
$$\left(\sqrt{\frac{T_{4}}{T_{2}}}\right)_{\text{Nopt}} = \left[1 - \sqrt{\frac{T_{2}}{T_{4}}}\right]$$

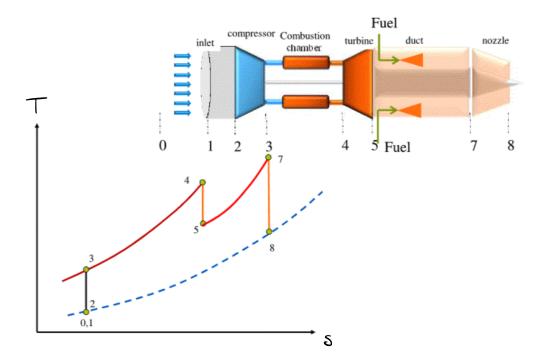
$$\left(N_{th}\right)_{Nopt} = \left[1 - \sqrt{\frac{T_2}{T_4}}\right]$$

# RADWINE CYCLE



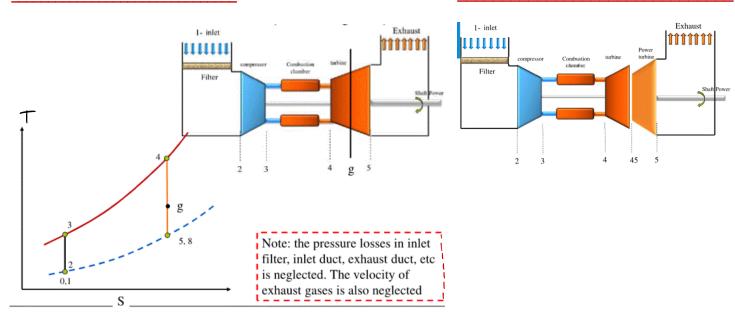
# Combined: BRAYTON AND RANGE





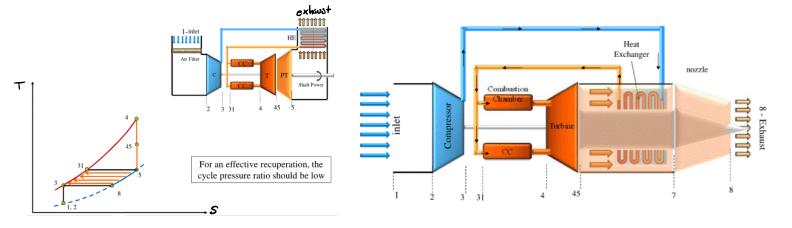


#### GAS TURBINE WITH POWER TURBINE



# Gas turbine with Recoperator:

# Jet Ensine with Resuperator: veg dificult.



# LECTURE 3 REAL BRYTON CYCLE

# · PEEVIOUS ASSUMPTIONS:

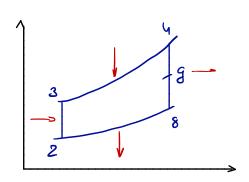
Constant Cp and Cv: ideal gas.

Constant mass flow.

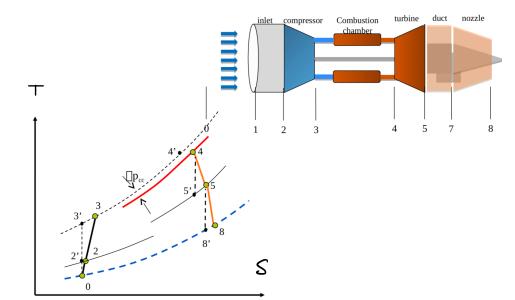
Adiabatic compression and expansion

No pressure losses in ducts and heat supply and rejection.

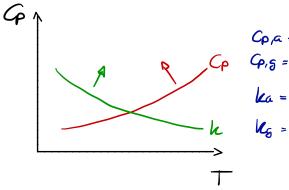
Une tic energy per component = 0



# REAL PROCESS



# Co and k reality:



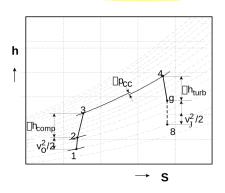
Cpa = 1000 7/45.k

CP, 5 = 1150 T/LS.K

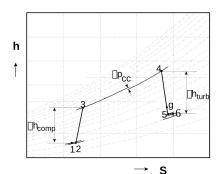
lea = 1.4 (before cc)

1.33 (from CC onwards)

# U-s diagram of jet ensine



U-s in a <u>stationary</u> gas turbine

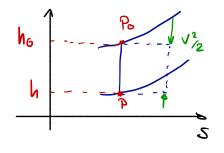


- · As Temperature increases:
  - K decreases: increasing fuel to air ratio. uis cooling increases
  - -> Co norcases: moreasing fuel to air ratio

# TOTAL PEOPERTIES

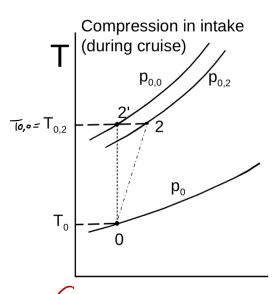
Total entholog: ho = h + 1/2 Vo2

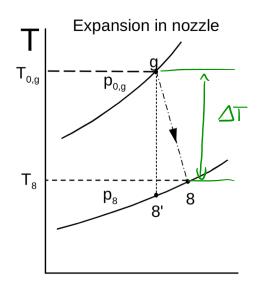
Total temperature: To = T + Vo2 ECP

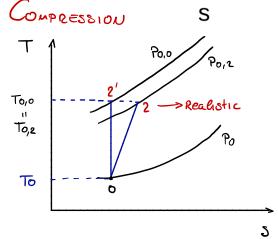


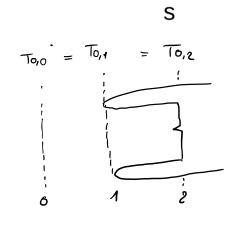
Total pressure:  $P_0 = P\left[\frac{T_0}{T}\right]^{\frac{k}{k-1}} = P\left[1 + \frac{V_0^2}{2C_PT}\right]^{\frac{k}{k-1}}$ 

#### NOW-ISENTROPIC COUPRESSION AND EXPANSION

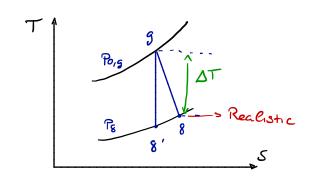


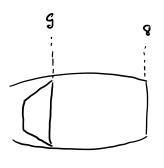






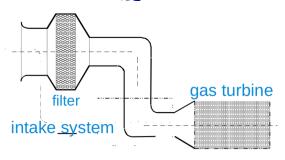
# EXPANSION



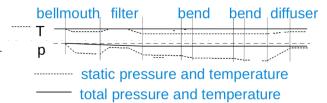


# STATIONARY GAS TURBINE INTAKE

 Pressure and temperature profile in the intake of a stationary gas turbine



· Total pressure stays the same, no energy added to the flow.



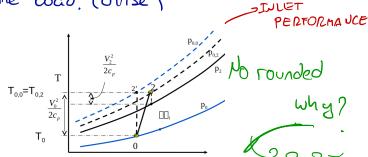
# AIRCRAFT GAS TURBINE INTAKE

external diffusion

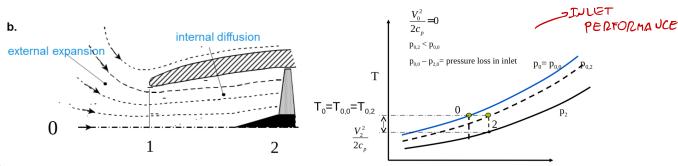
External and internal diffusion near an intake of an aircraft gas turbne.

a.) Uigh flight speed and low eighe load (crise)

internal diffusion



b) Low flight speed and high ensure load. (take-off)



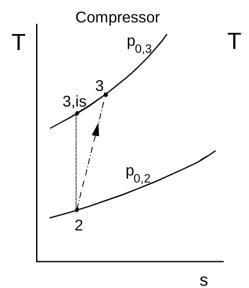
JULET EFFICIENCY

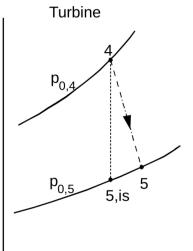
$$To_{12} = To + \frac{Vo^2}{2C\rho_{,a}} = To \left(1 + \frac{Va^{-1}No^2}{2}\right)$$

$$P_{0,2} = P_0 \left[ 1 + N_{in} \cdot \frac{V_0^2}{2C_{P,a}T_0} \right] \frac{h_a}{h_{a-1}} = P_0 \left[ 1 + N_{in} \frac{\kappa_a - 1}{2} N_0^2 \right] \frac{u_a}{\kappa_{a-1}}$$

# REAL PROCESS ROTATING COMPONENTS

#### COMPRESSOR



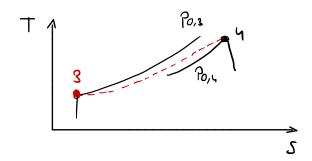


S

$$Nis,comp = \frac{\dot{U}comp,is}{\dot{U}comp,real} = \frac{T0,3,is - T0,2}{T0,3 - T0,2}$$

# Real CONSISTION CHAMBER:

Pressure drop: 
$$\Pi_{cc} = \frac{P_{0,M}}{P_{0,3}}$$



Essiciency: 
$$M_{cc} = \frac{\dot{m} \cdot C_{p,gas} \cdot (T_{0,u} - T_{0,3})}{\dot{m}_{g} \cdot L_{UV_{g}}}$$

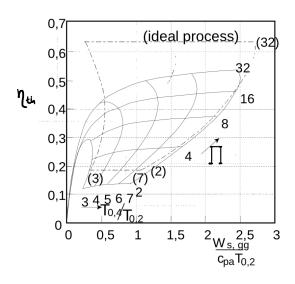
#### TURBINE

# COUNTING EQUATIONS AND

#### PARAMETERS

Parameters	$T_{o} - T_{0,g}$	5
25	$p_{o} - p_{o,g}$	5
	$\Pi_{\text{comp}}$ - $\Pi_{\text{cc}}$	2
Relations		1
	V <sub>o</sub>   m˙, m˙ <sub>f</sub> , LHV <sub>f</sub>	3
12	m, m <sub>f</sub> , LHV <sub>f</sub>	
	η inlet, η comp, η cc, η turb, η mech, η th	3
	$W_{comp}$ , $W_{turb}$ , $W_{gg}$	
		25
Design	To, Po, Vo, Flamp, Ta, in, Muler, Marp, Ma, Mert, Musch	
Design	TI cc , LHVI	(13)
Test bed	$T_{o}$ , $p_{o}$ , $T_{0,1}$ , $T_{0,2}$ , $T_{0g}$ , $\dot{m}_{f}$ , LHV <sub>f</sub> , $p_{0,1}$ , $p_{0,2}$ , $p_{0,3}$ ,	
	p <sub>0,g</sub> , η <sub> mech</sub> , η <sub> cc</sub>	(13)

# GAS GENERATOR WITH LOSSES



Specific power and thermodynamic efficiency of a sas generator with losses.

# From Maple Ta:

Single stage compressor replaced by intercooled multistage compressor and a reheater is used. (same peasure and temperature limits)

· Net work: increases.

· Neat rejected: increases.

Single stage compressor replaced by intercooled multistage compressor (some pressure limits)

· Compressor work; decreases

(Suel flow unchanged)

· Thermal efficiency: decreases

Single stage compressor and turbine replaced by intercooled, recupeated, reheated cycle.

Come pressure and temp limits ]

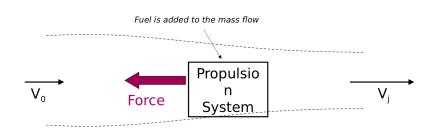
· Net work: Increases

· Neat reject: Decreases

# CUAPTER 4 AERO - ENGINES

# Propulsion

#### dINEAR MOMENTUM EQUATION



#### FORCE CAN BE CREATED:

Small amount of mass a large acceleration

- · A small acceleration to a large mass: Appeller. darge amount of mass a small acceleration.
- · A large acceleration to a small mass: Jet.
- · The mass can also be taken with you. Rocket.

Choice, what is the most Efficient?

- · Power available & \_\_\_ Total essiciony Notes
- · Jet Pover Pj -> Propulsive efficiency. Mprop
- . Thermal Power Q -> Thermal efficiency Nth

# POWER AMILABLE



Worh:

$$W = F \cdot \Delta V$$

W = T (X2-X1)

Power:

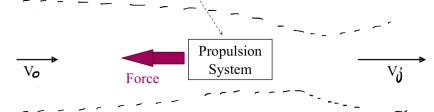
$$P = \frac{\omega}{\Delta t} = \frac{T(x_2 - x_1)}{\Delta t} = T \frac{\Delta x}{\Delta t} = Tv_0$$

Pa= TVo

JET POWER: Increase in lunetic energy of the flow.

Fuel is added to the mass flow

 $P_{0} = \frac{1}{2} \text{ m V}_{0}^{2} - \frac{1}{2} \text{ m V}_{0}^{2}$ 



# HERMAL POWER

Meat energy supplied to the process (burning fuel)

Q = Mg LUVg

# OTAL EFFICIENCY

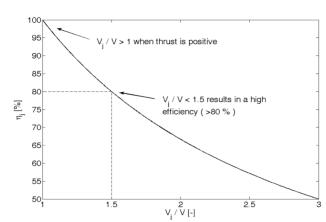
Ratio of Power available over Thermal power.  $N_{lot} = \frac{P_a}{\dot{a}}$   $N_{tot} = \frac{P_a}{P_J} \cdot \frac{P_J}{\dot{a}} = N_{prop} \cdot N_{th}$ 

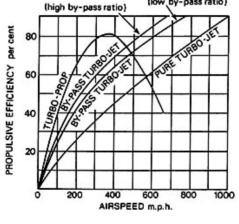
# PROPULSIVE EFFICIENCY

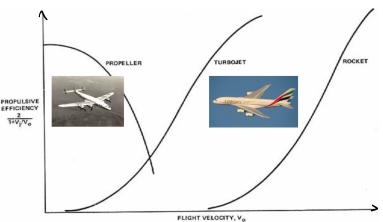
$$\eta_{\text{prop}} = \frac{P_a}{P_j} = \frac{2}{1 + \frac{V_j}{V_o}}$$

#### · CONCLUSIONS:

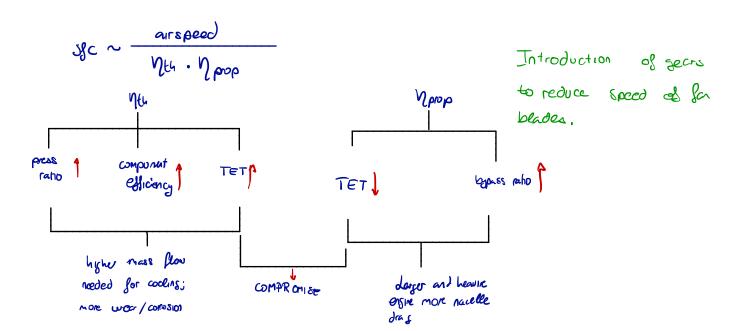
- · Taster speeds become more essicient.
- · dower speeds: propeller. (turboprop)
- · Visher speeds: jet ensine.







# DESIGN CONSIDERATIONS



# USEFUL DEFINITIONS

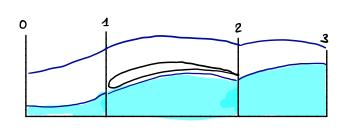
#### Thrust

# Essiciency

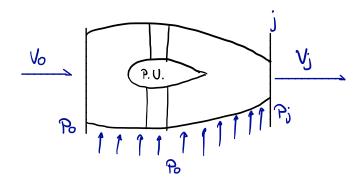
$$\eta_{tot} = \frac{P_a}{Q} = \eta_j \cdot \eta_{th}$$

$$\int \rho r o \rho = \frac{P_a}{T_j} = \frac{2}{1 + \frac{V_j}{V_j}}$$

# A CLOSER DOOK INTO THRUST



# COMPOSITION OF THRUST



# Thrust = m (Vj - Vo) + Aj (Pj -Po)

OROSS THRUST: FG = E[m V, + A; (P; -Po)]

Not Thrust: For = E [m (Vj - Vo) + Aj (Pj - Po)]

Specific Thust: To = F/m

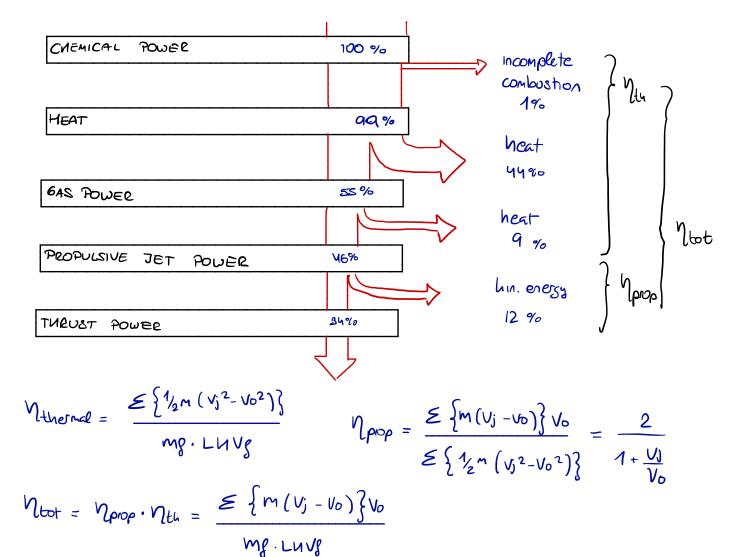
Specific fuel consumption: 
$$Sfc = \frac{mg}{F_{N}}$$

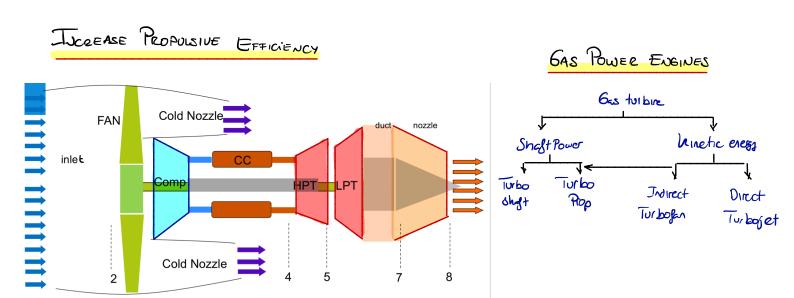
# JET ENGINE POWER AND LOSSES

Jet Power: Wprop.jet = 1 m (Vj 2-Vo2) Power doss: Plass = 1 m (Vj-Vo)2

TURNET POWER: WITHUST = M (VJ-VO) VO

# JET ENOINE SAUREY DIAGRAM



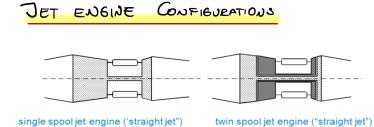


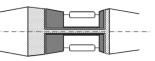
Turbajet: all air through combustion chamber

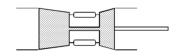
Turbofan: bypass, mixed us. separate ehoust norseles.

Turbo prop: propeller + exhaut get turist. See vs. fixed power burbine.

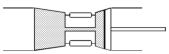
Single us nultiple shift ensines.





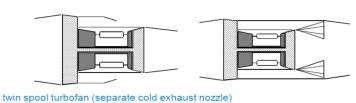


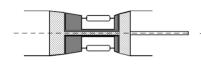
Turboshaft (-prop) CONFIGURATIONS

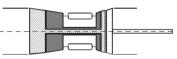


single spool turboshaft

twin spool (free turbine) turboshaft





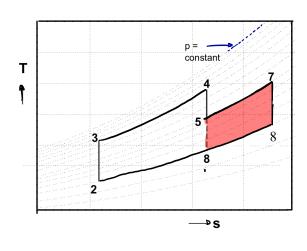


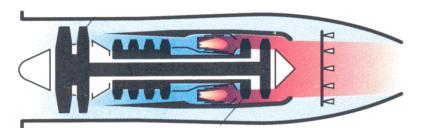
twin spool 'mixed' turbofan

twin spool gas generator / turboshaft

triple spool (free turbine) turboshaft with twin spool gas generator

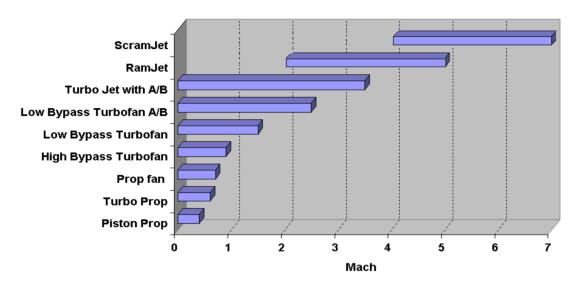
#### AFTERBURNER:



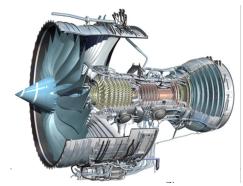


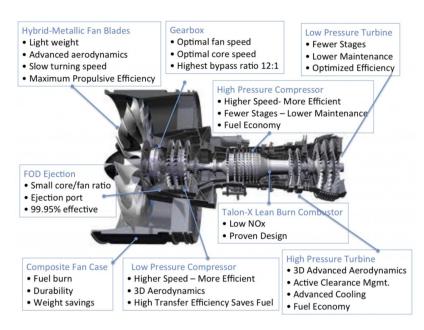
The ensure burns much more fuel than in the whittle engine and occupies much less volume than the earlie combustion chambers

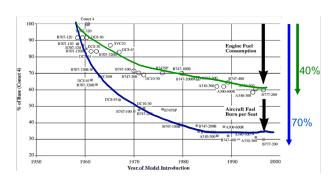
# WHY SO MANY ENGINES ?

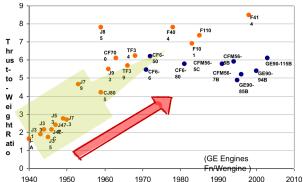


#### TURBOFAN 3 Spool









TURUST

# EUGINE JUTAKE SYSTEM

#### CONSTRAINS

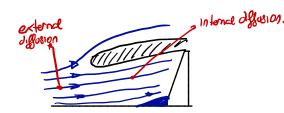
- · Ensure Operation / Control
- . FOD containment
- . Noise

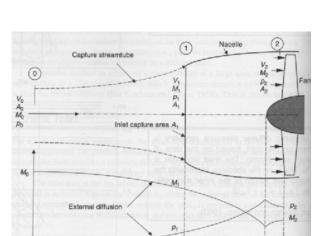
· Co8+

- . Weight, Size, gound clearance
- · Minimizing Pressure doss, dras
- · RCS/IR

#### IN FORMATION:

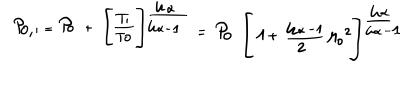
- · Esentially a fluid flow duct whose task is to process airflow in a way that ensures that the ensure functions properly.
- · Provide adecuate amount of uniform airflow
- · Crusing: conversion of Estin into Epot (prossure)
- · Ran compression / "Ram recovery"
- Supersonic vs. subsonic intale
- · "Bellemouth" intake (test bed /stationary)
- · Subsonic inlets are dominated by the boundary layer behaviour.
- . Supersonic inlets are dominated by the shock stucture.

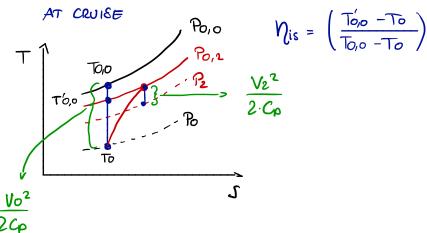




$$T_{0,1} = T_0 + \frac{V_0^2}{2C_p} = T_0 \left[ 1 + \frac{k\alpha - 1}{2} n_0^2 \right]$$

$$R_0 = R_0 + \left[ \frac{T_0}{2} \right] \frac{k\alpha}{k\alpha} = 0$$





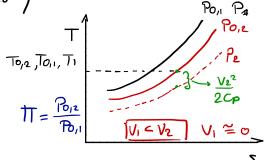
$$N_{ran} = \frac{P_{0,2} - P_0}{P_{0,0} - P_0}$$
 easier to measure

Nis and Yram can be used intorcharscable till M < 0.8

# SUBSONIC INTAKE

a) Rest

b) Static + crosswind c) dow-speed flight.



# ENGINE EXHAUST SISTEM

- Minimiting Pressure Coss, dras
- · Thust vectoring / Reversins · Minimizing weight, size

Cost

- · Norse
- Engine operation/control
- RCS/IR

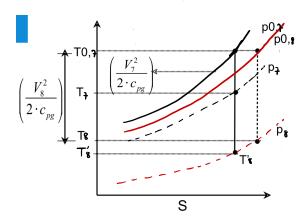
#### JUFORMATION:

- · Accelerate the flow to a high relocity with minimum pressure loss
- · Match exit pressure to atmospheric, as closely as possible
- · Suppress jet noise
- . Permit control of the ensure operating characteristics.

#### JUFORMATION (CNID)

- · Permit afterburner operation
- · Mix core and bypass streams of turbofan if necessary
- · Allow for thrust reversing is desired
- · Thrust Vectoring control
- · Suppress radar cross-section
- · Suppress infrared emision.
- . Minimize cost, veight and drag while meeting reliability.

#### NOTHE EFFICIENCY;



#### dosses:

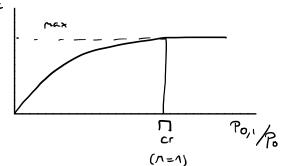
- · CD: discharge coefficient = Aell/Ageom ~ 0.95 0.97
- CD: viscologie acquired.

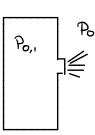
   CV: velocity coefficient = Viet/Viet ideal N 093-098 } smile loss.
- · CX: Thrust coefficient = F6/F6 word ~ ags 0.98

#### THEUST LOSS:

- . Due to the exhaust velocity applicatly.
- · Due to the exhaust swirl
- · Due to loss of mass due to lealinge.
- · Due to reduction in the velocity magnitude consed by friction.

#### CRITICAL PRESSURE RATIO





COMPLETE EXPANSION Calculation recipe for unchocked norrele

$$\frac{P_{0,1}}{P_{0}} \leq \prod_{\sigma}$$

$$\frac{P_{0,1}}{P_0} \leq \prod_{\sigma} \qquad P_{jet} = P_0 = P_{atm} \qquad T_{0,1} - T_{\ell} = T_{0,2} \cdot \eta_{1,3}, n_{0,2} \qquad 1 - \left(\frac{P_0}{P_{0,1,2}}\right) \frac{n_{\ell} - 1}{n_{\ell} s}$$

$$P_{jet} = P_0 = P_{Ath}$$
  $V_{jet} = \sqrt{2C_{P_{j}}(T_{O,?} - T_{8})}$   $F_{N} = v_{1} \cdot (V_{8} - V_{0})$ 

INCOMPLETE EXPAUSION Calculation recipe for chocked notable.

$$\frac{P_{O,1}}{P_{effn}} > \prod_{\sigma} = \frac{1}{\left[1 - \frac{h_{5} - 1}{\gamma_{is,nos}(h_{5} + 1)}\right]} \frac{h_{5}}{h_{5} - 1}$$

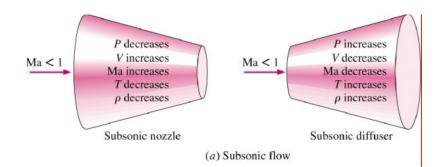
$$\frac{P_{6} = P_{0,4}}{T_{6} = P_{0,4}} / \prod_{\sigma} \sigma$$

$$T_{6} = T_{0,7} / T_{6} \sigma$$

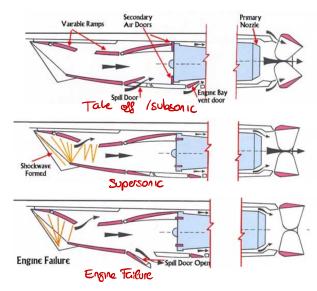
$$T_{6} = \frac{\mu_{6} + 1}{2}$$

$$TRcr = \frac{k_b+1}{2}$$

#### COMPRESSIBILITY:



# Turbojet concorde -> Rolls Royce-Snecma Olympus 593 /Variable geometry intake.



General characteristics at ISA take off conditions

Compressor= 2 spool axial, 7 low pressure stages, 7 high pressure stages

Turbine= Single stage high pressure, single stage low pressure

Nozzle= Convergent

LPC Pressure Ratio = 4.0 HPC

HPC Pressure Ratio = 4.0

Bypass Ratio = 0

Ambient Temperature = 288 K

Combustor Exit Temperature  $(T_{0.4}) = 1450K$ 

Combustion efficiency = 0.99

Intake Pressure ratio= 0.92 (at take off)

Combustion chamber Pressure Ratio = 0.97 Afterburner Pressure Ratio = 0.97

Afterburner efficiency = 0.95 Afterburner Exit Temperature  $(T_{0.7})$  = 1850 K

Engine mass flow rate= 160 kg/s

Compressor isentropic efficiency = 0.85 Turbine isentropic efficiency = 0.9

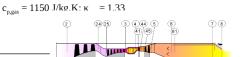
Mechanical efficiency = 0.99

Nozzle efficiency = 0.95

 $c_{p,air} = 1000 \text{ J/kg.K}; \kappa_{air} = 1.4$ 

Gas constant= 287 J/kg.K Fuel calorific value = 43 MJ/kg

Ambient Pressure = 101,325 Pa



# · Inlet persure ratio is 0.92 at take off

$$\frac{T_{0,2s}}{T_{0,2}} = 4 + \frac{1}{\eta_{us}} \left[ \left( \frac{\rho_{0,2s}}{\rho_{0,2}} \right)^{\left( \frac{4-1}{\omega} \right)} - 1 \right]$$

$$\frac{T_{0,2}}{T_{0,2}\epsilon} = 4 + \frac{1}{\sqrt{i_s}} \left[ \left( \frac{2b_{,3}}{P_{0,2}\epsilon} \right)^{\left( \frac{L-1}{2L} \right)} - 1 \right]$$

#### · Combustion Chamber:

· Afterburner:

$$P_{0,7} = P_{0,8} \cdot 0.97 = 379233.79 Pa$$
 $P_{0,7} = P_{0,8} \cdot 0.97 = 1850 \text{ Given}$ 
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 $P_{0,7} = P_{0,8} \cdot 0.97 = 1850 \text{ Given}$ 
 $P_{0,7} = P_{0,8} \cdot 0.97 = 1850 \text{ Given}$ 
 $P_{0,7} = P_{0,8} \cdot 0$ 

· Notrle:

$$\frac{P_{0,1}}{P_{0,1}} = \left[ \frac{1}{\left(1 - \left(\frac{1}{N_{000}}\right) \cdot \left(\frac{L_{5} - 1}{L_{5} + 1}\right)\right) \frac{L_{5}}{u_{5} - 1}} \right] = 1.916 \qquad \frac{P_{0,2}}{P_{0}} = 3.94$$

$$(<) \implies crocked!$$

$$F_{8} = T_{0,9} \cdot \left(\frac{2}{L_{5} + 1}\right) = 1589.98 \text{ K} \qquad P_{8} = P_{0,9} \left(\frac{1}{P_{0,p}}\right) = 16961$$

$$P_{8} = \left(\frac{P_{8}}{R \cdot T_{8}}\right) = 0.434 \text{ Lights} \qquad V_{8} = \sqrt{L_{5} \cdot R \cdot T_{8}} = 998.56$$

$$A_{8} = A_{001} = \left(\frac{m}{P_{8} \cdot V_{8}}\right) = 0.463 \qquad F = \text{vis} \left(U_{8} - V_{0}\right) + A_{8} \left(P_{0} - P_{0}\right) = 199.41 \text{ Lights}$$

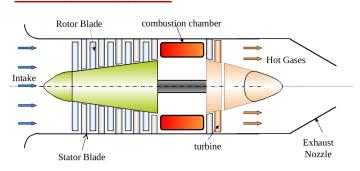
$$SFC = \left(\frac{\text{mfrel}}{F}\right) = 37.78 \text{ sm/hv·s}$$

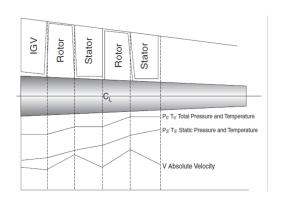
FOR TURBOPROP LOOK IN THE SLIDES

# LECTURE 6 TURBOMACHINERY

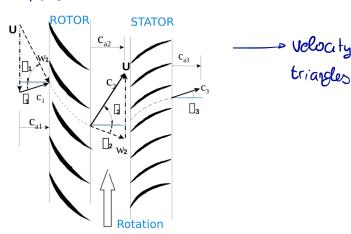
Rotating equipment that performs work on a fluid or extracts work from a fluid.
Types of Compressors:

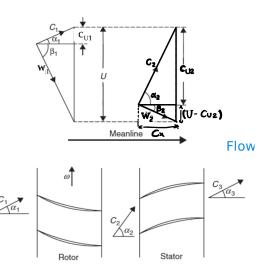
#### AXIAL COMPRESSOR

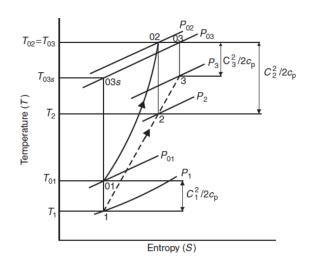




#### FLOW PATTERN







#### Euler Formula:

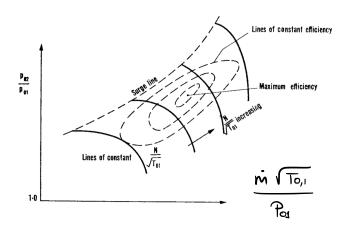
1. F=M2·CU2 -M1·CU1 → force exerted on Ne fluid.

2. t = M2. Cu2. 12 - M1. Cu1. 1, -> torque exold on fluid.

3. W= t·W - Torgue x Angular velocity
Power input to he fluid.

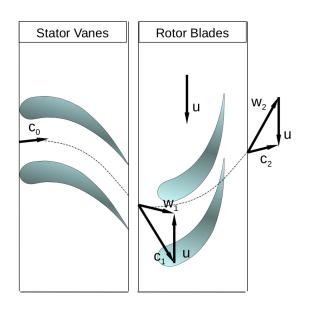
4. W = U0,2 - H0,1 = M (CU2 U2 - CU1. U1)

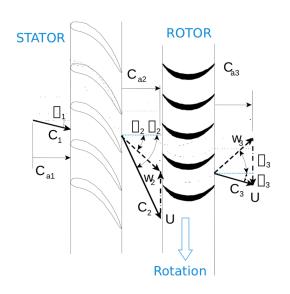
WSP - 17hout m = N2-11



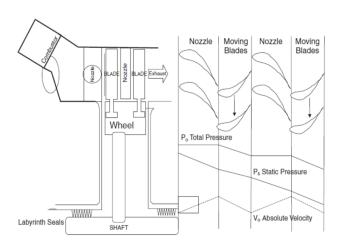
#### Research units Multi-stage industrial 0,92 Multi-stage Single stage 0,90 0,88 0,86 Multi-stage Gas generator 0,84 Multi-stage fan Single stage fan 0,82 1,6 1,8 1,0 1,2 1,4 2,0

# AXIAL TUEBINES





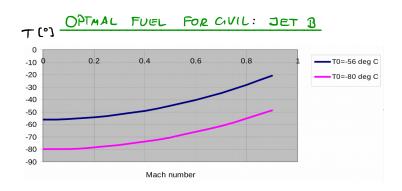
PRESSURE RATIOS



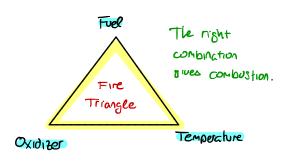
# COMBUSTION

#### KEROSENE AS AVIATION FUEL

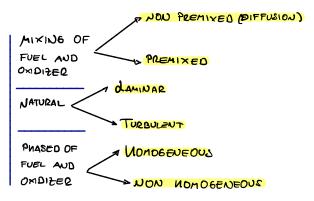
- · Dresel problem, it can freche after 5 hm altitude.
- · Kerosene maximum Prene point is: -60°C sood.
- · Clean combustion . Good energy density
- · 6000 hemal stability



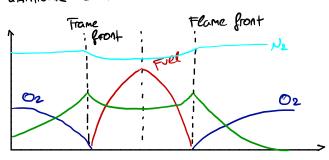
COMBUSTION: exothermic oxidation process (jet engines supposed a revolution)



CLASSIFICATION:



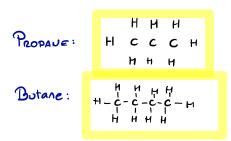
DAMINAR DIFFUSION FLAME



There is a difference between combustion and fire!

CONBUSTION STOTEMIONETEY: balance the equations to find how much origin we need, so how much air.

#### GAS COMPOSITION



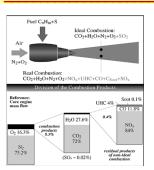
#### FUEL TO AIR RATIO

Rich mixture: more fuel than air  $\phi > 1$ .

Lean mixture: more air than fuel.  $\phi < 1$   $AF = \frac{Mair}{Mpuel} = \frac{1}{FA}$  — fuel to air ratio.

AFTER COMBUSTION:

#### KEROSENE AS AVIATION FUEL

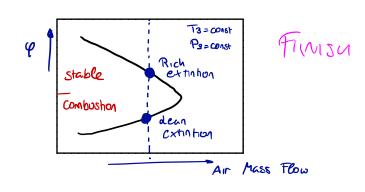


Engine Family	Aircraft	Take-Off Thrust, [kN]	Overall <i>AFR</i> at TO	Overall $\varphi$ at TO
CFM56-7	B737 NG	91.6	54.0	0.27
RB211-535	B757	163.3	52.3	0.28
CF6-80E1	A330	297.4	49.3	0.30
PW4000- 112"	B777	396.6	43.1	0.34

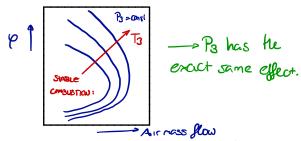
# MEAT OF REACTION Chemical View Products To Ti

Temperature

#### FLAMABILITY DIMIT



#### EFFECT OF TEMPELATURE ON THE FLAMMABILITY



At the moment, we reduced the size of chambers a Cot.

#### COMBUSTION CHAMBER REQUIREMENTS

- · Migh combustion essiciency over wide operating conditions.
- . dow pressure loss over the combustion system.
- . Stable combustion over a wide range of inlet conditions and mass flow
- · Wide range of equivalence ratio coperational reliability)
- · Reliable starting copability coperational reliability)

- · exhaust emmission consistent with regulation.
- · MINIMUM Persth
- . dow cost and good durability, maintainability reliability (cost)
- dons operating life (ensue life)
- · Combostor exit temperiore patton (ensine life)
- . Multi-fuel capacity. (in future)

#### CONVENTIONIAL COMBUSTOR

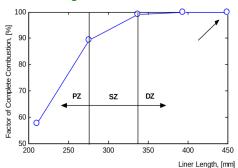
#### Primary zone:

- · Anchors the flame
- · Provides sufficient time, temperature and turbulence.

#### Three step process:

- · Endothermic dissassociation of fuel
- · Exotheric formation of co 8 U2O
- . Exothermic conversion of co to CO2

#### Factor of complete combustion.

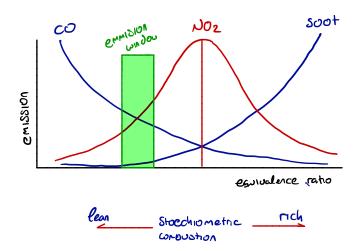


# Primary zone of the combustor:

Temperature distribution: 2400 2200 2000 Mean Static Temperature, [K] 1800 1600 Mixing 1400 Chamber D7 1200 1000 800 L 150 250 300 350 400 Wall Length, [mm]

The air around stabilizes the flame when its close to the ord.

#### EMISSIUN



#### COMBUSTION PERFORMANCE

efficiency: 
$$\eta_{cc} = \frac{(\dot{m}_a + \dot{m}_s)_{cb} \Delta T}{\dot{m}_s Luv_s}$$

$$\Pi_{cc} = \frac{P_{0,4}}{P_{0,3}}$$

#### pressur losses:

$$D \rho_{3,4} = D \rho_{\omega} \omega + D \rho_{\phi} + D \rho_{\phi}$$

$$D \rho_{\phi} + \frac{C V^2}{2} \times \frac{T_4}{T_2} - 1$$

#### TYPES OF COMBUSTION CHAMBERS

Elements and aspects

**→** ∂1**%**0&er

- wall and lining

→ coolng

· Build in configurations

- can type

- annular type

-> cannular type

→ revese flow

#### TMPACT OF AVIATION IN THE ENVIRONMENT

No offect on the Stratosphere, but in the troposphere the release of CO2, NOx, produces Change. At Ground Cevel, he most concurred problem 16 the sound.

Jet fuel consumption beeps growing.

#### ALTERNATIVES:

Electric motors, hydroson, utilitary aircraft

# ELECTRICAL POWER SYSTEMS

· Provides power to several compounts in the vehicle.

Aircraft (combination)

REQUIREMENTS:

· Power types: Alternate current or Direct current non constant and constant voltage.

Spacecraft

- · Voltage and airrest level: For AC: root mean square (rms) are given.
- Frequency and number of phases: for AC only Future DC systems with high voltage.

reducts he size of behide,

DEFINE SYSTEM POWER OF AC SYSTEMS

Apparent Power Pappa = V. I -- current

EXERCISE:

500 hVA at PF = 0.8

(4) Actual Power? 400 hk (2) Work of 8 hours, total energy?

Pactual = Papparent. PF

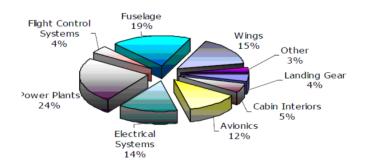
ETOTAL= PACTUAL · LIME

POWER ON AIRCRAFT: new-generation spacecraft and aircraft heavily rely on electrical power. Spacecraft use very little power compared to aircraft.

HOW YUCH ELECTRICAL POWER IS NEEDED

3 to 5% total power is not used for propulsion. In airorft 0.45 to 1%

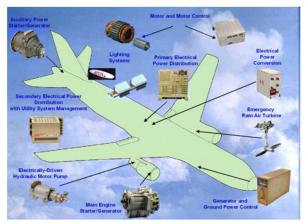
FUTURE 1



Power User	Comments	Typical Power Level	
Air Conditioning	ECS	4 x 70 kW+	
Flight Controls	Primary & Secondary	3 kW to 40 kW	
		short duration at high loads	
Fuel Pumps		About 10 kW	
Wing Ice Protection	Thermal mats or similar	250 kW+	
Landing Gear	Retraction, steering and braking	25 kW to 70 kW short duration	
Engine Starting	May be used for additional applications	200 kW+ Short duration	

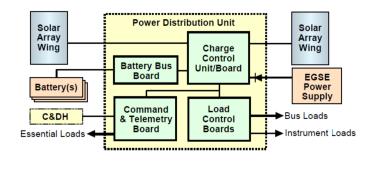
#### RELIABILITY ISSUES:

- . In aircrafts is good 099997
  - · In space launchers 0,992
    - · In spacecrafts 0.87



#### 2TUBUCHAC)

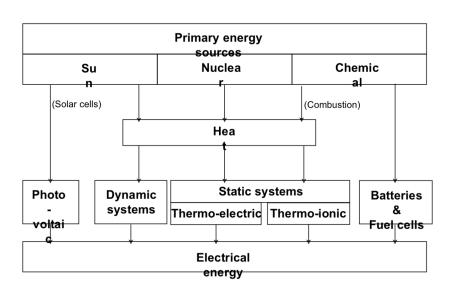
· Function is to generate, regulate and distribute the electrical power throughout the wehicle.



# ENERGY SOURCES:

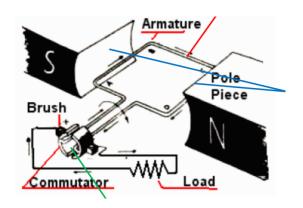
- External Sources: Outside uchicle. mass/cost/ 512e budget out of the vehicle.
- · Internal Sources: Stored or produced inside the vehicle. Autonomous vehicle.

# POWER GENERATIONS:



# DYNAMIC ELECTRIC GENERATORS

- · Electromagnetic induction systems capable to convert hinetic energy into electrical energy.
- · In aircraft, or driver by the engine through a belt.

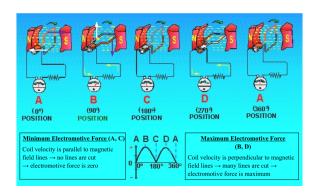


- (1) Rotating coil: input Linetic energy is used to rotate it at a siven speed.
- (2) Stationary magnetic field: produced by permanent magnets or electromagnets.
- (3) Semi-cylindrical contacts; produce a constant-direction electromotive force

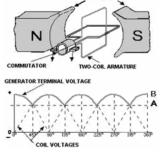
Rotating coil causes the Acternate current.

- · Minimum force: coil velocity is paralled to magnetic field.
- · Manmon force: coil velocity is perpendicular to magnetic field.

Conmutator males that sinusoidal wave is always in the same direction.



#### DILECT CURLENT GENERATORS



- Introduce a second Connutator to reduce MINIMUM
- · Each coil is comeded to the load circuit when the electromotive force is higher.
- · Four coils produce reasonable constart voltale

#### AC GENERATORS:

- · Same as a DC generator: without commutator.
- · Two options:
  - → Rotating currature
  - Rotating magnetic fleed.
- " Belt driven or axis driven. smple, lighter and cheaper.
- · Provide sufficient power at law rotating speed.
- · Constant speed: synchronization with electrical frequency. Or add controls.

# BASIC EQUATIONS (PERFORMANCE)

# Electromotive force produced: E

- · N number of windings (turns) of coil
- · B masnetic field strength. Text
- · A Arca enclosed by a angle turn
  - · W rotational speed. rad/s

# Output voltage:

- · I Current in the circuit
- · Ran Internal resistance of the armature

#### Power P.

$$P = T^2R = \frac{V^2}{R}$$
 \_\_\_\_\_ time dependent: \_\_\_\_ remove it using average power.

EFFICIENCY OF GENERATOR

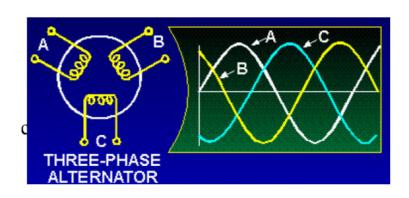
# OUTPUT FREQUENCY

$$g = \frac{h \cdot P}{120}$$

- · n rotating speed (rpm)
- · P number of magnetic poles.

# MULLI PUASE ALTERNATORS

Two or more symmetrically spaced coils present. Each coil produces a phase shifted AC voltage. (3 are tupically used) Produce a phase shift of 120°



Smaller and cheaper.

Vens = 13 · (Vens) single phase.

# DRIVE SYSTEMS

. Use the internal combustion ensures or the ram our turbines.

- · Also use a solar dinamic drue system. Son heats gas, gas moves terbire.
- . The drue system input power is higher than the generator input power.

Connection Solween generator and once. (90 to 95%)

# STATIC ELECTRIC POWER GENERATORS

· THERMOELECTRIC CONVERTERS (TEC) two different metals or semiconductors connected in a closed loop. If they are at different temperatures a potential is generated between them.

(See beach effect) Peltier cells: opposite.

PHYSICAL LIMIT: NEVER ULGHER THAN CARNOT EFFICIENCY

- THERMO-JONIC CONVERTERS: (TIC) wessel containing two metal electrodes (plates)

  with an ionitable gas between them. The hot electrode is heated at 1400-1800 k and

  causes contration of the gas. between the plates. Gas garates voltage difference. (0 to 25% efficiency.
  - PLADIO ISOTOPE THERMAL GENERATOR: (RTG) Power obtained from the radioactive decay of a radio-150 tope material. Weat is converted to electricity. Deep space missions would.

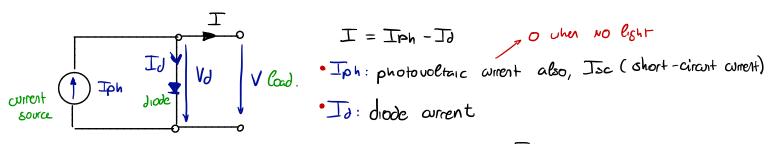
# PHOTOVOLTAIC GENERATORS:

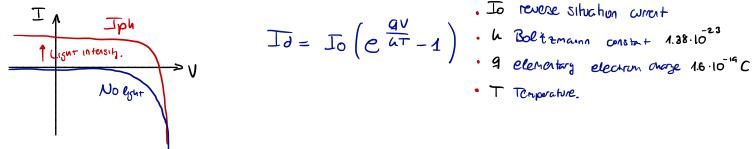
Primary energy source of spacecraft. Available at no cost, unlimited and external. Depends on Sm.

· Solar cell: semiconductor diode: electronic component that conducts ament only in on direction.

Autorial that is an insulator at absolute two temperature but conducts electrically at room temperature.

- · A p-n junction is obtained by connecting two different types of semiconductors:
  - · A positive charge courier (ptype)
- When illuminated, electrons are released.
- · A negative charge carrier (n-type)
- If the circuit is closed, a current flows in it.
- \* Solar cell: ourrent source in parallel with a diode.





$$T_{\partial} = T_0 \left( e^{\frac{qV}{4T}} - 1 \right)$$

- . To reverse situation current

- · Pmax = Vmpp · Impp = Voc · Isc · FF

Power Delivered (I=0)

P= V.I open and Curet IN wrue of the solar cell Voltage

>maximum pover point

FF: Fill factor: FF = 4 when

I-V curve shape is completely rectangular.

EFFICIENCY:  $N = \frac{P_{max}}{P_{in}}$  -> It can still be improved, max of 44%

# PHOTOVOLTAIC MODULE

Made of solar cells connected in series and in parallel.

- · Noells in series form a strins.
- } Connected cells have the same IV curves
- · M cells in parallel form a module.

Vanous modules together form a solar array.

Single cell voltage Vcell  $\}$   $\longrightarrow$  V cells in sures:  $\}$   $\longrightarrow$  A cells in parallel A single cell curent A cells in A cells in A cells in parallel A A cells in A cells in

# EFFECTS OF CELLS AND STRINGS FAILURES:

- "Open-circui+ failure of a single cell:
  - -The entire string Pails.
  - Auoid by including shunt diodes.
- · Short-airait failure of a string:
  - dower string voltage
  - -> Penerse current might occur, higher lemperatura in the cells.
- Avoid by including blocking diodes.

# PERFORMANCE AND SIZING

- . The efficiency of the solar cells in space is 1 to 3 90 lower. Efficiency is based on a reference temperature of 25°C
- Variations of the I-V wrve with temperature are expressed by the Temperature Cooperations.

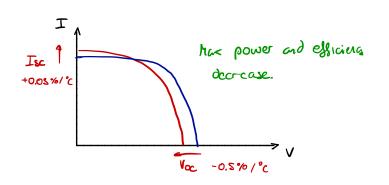
EFFECTS OF TEMPERATURE

· Increase of Temperature:

Short circuit cirrent slightly increases.

Open aircuit voltage significantly decreases.

 $Voc(T) = Voc(T_0) + d(T-T_0)$ 



- \* Operational range -60°C to 55°C
- · Thermal control is needed. Back surface reflectors, Filters cit out the energy of wowelers this.

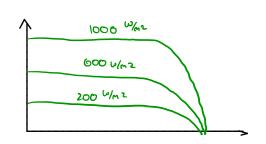
EFFECTS OF AGEING

Caused by high energy radiations. Also by atonic oxiger, thernal cyclis, micrometeoroid smles.

Total life degradation: 
$$L_d = (1-\delta)^{\times} \rightarrow P_{X-years} = L_d \cdot P_{BOL}$$
8 is the yearly power degradation and call power at begginns of

EFFECTS OF SOLAR FLUX:

Depends on distance from the SUN.



JUFWENCE OF INCIDENCE ANGLE

Depends on influence Arca

Ae = A · cos (0) - maximum for perpendicular.

EFFECT OF SOLAR RADIATION SPECTRUM:

- · Solar radiation depends on height, decreases when in the atmosphere.
- · Efficiency of the cells on Space is higher than in space.
- The air mass coefficient DM is defined as 1/coso o: engle between the solar radiation direction and the earth surface.

AVAILABLE SOLAR ARRAY POWER

Psa = Sin · A· N · Id · Cos (O)

Incident egicing life

Solar of solar degradation degrada

# SOLAR ARRAY DUTY CYCLE AND REQUIRED POUBL

Nominal Power power during day power during night

Power of the power during night

Power during day power during night

# LECTURE 10 ELECTRICAL POWER SYSTEMS

## BATTERIES: series of voltaic cells

voltaic cell: two electrodes made of different materials inmersed in a conductor.

— cathode: positive electrode also called a constant voltage

anode: negative electrode source.

Chemical reactions in the cell generate a voltage difference between the electrocles. When connected to a load, wirest glows from the cathode to the anode.

BATTERM CHARACTERISTICS - CELL VOLTAGE

- · Voltage decreases during discharge.
- · Voltage is strongly dependent on the obenistry and the materials.
- · Nominal voltage voltage at 50% discharge. (MPV) mid point voltage
- · End of discharge voltage.

### TYPES OF BATTERIES:

- · Wet Cells: liguid electrolyte
- · Dry cells: paste electrolyte.
- · Primary: non rechargeable
- · Secondary: remargeable
- The voltage of a battery while charging is different to its voltage during discharge.
- · Cell capacity: total ammount of energy that a cell can deliver.

$$C = \frac{E}{V} \longrightarrow \text{botal amount of energy.}$$
 [A/h]

· RATE DISCHARGE CURRENT: conditions

$$T = \frac{C}{t_D} \rightarrow discharge time for a different discharge time, capacity will not be assumed.$$

• SPECIFIC ENERGY = TOTAL ENERGY

CELL MASS

Nominal capacity: conditions

- · Total discharge tre
- · Discharge temperature
- · End-of-discharge voltage

ENERGY DENSITY = TOTAL ENERGY
CELL VOLUME

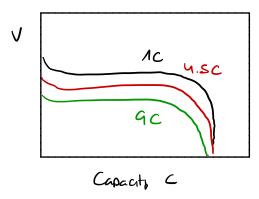
### C-RATE OF A CELL

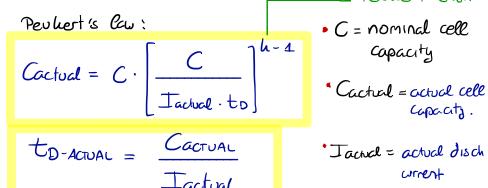
- Indication of its raled discharge time.
  - $C=1 \rightarrow discharge$  rate of 1 hour .  $\frac{C}{2} = 2 \text{ hours}$  .  $2C = \frac{1}{2} \text{ hours}$ .
- Indication of the rated discharge current.

$$T = C/t_D$$
  $\longrightarrow$  C-RATE =  $C/3$   $\longrightarrow$  3 hours  $\longrightarrow$  for  $C = 6 \longrightarrow 2A$ 

### EFFECTS OF DISCHARGE WRIENT:

· Ig a cell is discharged at a current higher than its rated discharge current, the actual capacity of the cell is lower than the nominal capacity.





C = nominal cell

- Peuhert Cast.

\*Jacual = actual disch whent

> to = nominal disch time

### EFFECTS OF TEMPEDANULE

- · Cell capacity decreases when temperature decreases.
- · Tipically: 1% per each oc below nomind rated temperature.

Thermal control 18 I important!

### CELLS IN SECIES AND PARALLEL

- · Battery is the connection of cells in series.
  - "Series: C = same V= N. Vcell
- · Connectors in parallel multiple battories forms an array
  - Parallel: V = Same  $C = N \cdot C$  batt

### CHARGE / DISCHARGE EFFICIENCY

#### CYCLE LIFE OF A BATTERY

- · Each charge / discharge gille reduces the capacity of a battery.
- · CYCLE LIFE: number of complete cand of that can be performed before the capacity falls below 80% of the initial value.
- · Typical around 500-1200 cycles.
- · To extend the gille life it is possible to reduce its Depth of Discharge.

how much the battery is discharged at each cycle.

### BATTERY SITENS

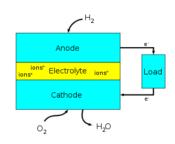
- · Pload: Average power regimed by the load.
- · top: max operational time before recharging.
- · Ntot: Total efficiency (discharge efficiency x transmission)

tran dry mass

- · VCoad: doad voltage
- · DoD: Depth of Discharge

## FUEL CEUS

- · Fuel cells produce electrical energy from chemical reaction
- One reactant (hydrogen) flows through the anode and gues electrons, the other reactant (oxigen) flows through the cathode and receives electrons.
  - A fuel cell can not be revsable.



### CUARCACTERISTICS

- Typicall efficiency of 40-60% Uigher power lower efficiency. space: reactions mass is 10-20 times higher
- · Tipically used for high-power loads (1-10 hw)
- · Uguer specific energy than batteries, same energy with lower mass, se = Total energy Cell mass

Sizine: wasider two parameters.

· Specific power: cell dry mass.

· Specific energy: cell reactants only.

CAPACITORS: characterized by similar characteristics as batteries.

- · Made of two conductors insulated from each other by a dielectric.
- . Store electrical energy and provide it back when connected to a load
- · No chemical energy conversion lates place
- · Faster discharge Than on batteres.
- · CAPACITANCE: amount of charge.

$$C = \frac{Q}{V} \rightarrow \text{olectrical charge}$$
 $C = \frac{Q}{V} \rightarrow \text{oltage difference}.$ 

· ENERBY :

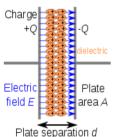
$$E = \frac{1}{2}CV^2 = \frac{1}{2}QV = \frac{Q^2}{2C}$$

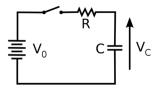
- · Capacitace depends on:
  - · Ageing and cycling
  - · Temperature
  - · Discharge wirent

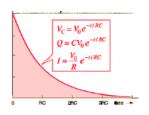
· DISCUARGE

- Vc (t) = Vo · e<sup>- ½c</sup>
- ► Q(t) = CV0e RC









# · Connecting N capacitors:

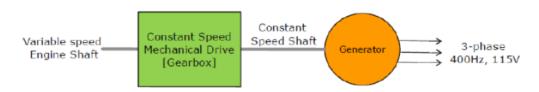
- · Seeies:  $\frac{1}{C_1} = \frac{1}{C_1} + \frac{1}{C_2} + \dots + \frac{1}{C_N}$
- Parallel: CT = C1+C2+....+ CN

# POWER MANAGEMENT

- · Used to adapt the electrical power to the type of local that it uses it.
- · Because of different voltage / current
- · Extends age of a device by forcing it to work under more comfortable 4 conditions

### ALTERNATORS

- · An usual requirement of Ac devices is to receive power at constant frequency.
- · Energy source, operales at variable speed
- · USE | INTEGRATED DRIVE GENERATOR | (ID6)
  - -> Constart Speed Drive, installed between the organe and generator
  - -> The CSD, hydro mechanical device.



· USE IVARIABLE SPEED CONSTANT FREQUENCY I CONJUTES.

Made of electronic components (ACIDC Converter + DC/AC one)

### SOLAR ARRAYS:

- . The I-V write and the maximum power change over time.
- · A voltage regulator is used to control this.

### ON/OFF SWITCHES

- . The only available control is on the number of array strings that are connected to the load.
- · Current can not be controlled.

### SERIES REGULATORS;

An adjustable resistance is installed in sense between the solar array and the bood. Vin Now Vout

Vout = Vin - Rs : Thood I local can also be adjusted.

Local can also be adjusted.

Local can also be adjusted.

Pin = Vin . ILDAG

Pdiss = Re. ILDAO 2

## SHUNT REGULATORS:

- · Smaller excess power is dissipated in the regulator. higher efficiency.
- . Shunt regulators make use of Zener dodes (allow for current in reverse direction)
- · Vout = Vin R. (ILOAO + ID) (R: fixed regulator resistance)

  (Io: current in the diode)

To allows for dissipation of excess power in he low resistance diode circuit.



Zener diode characteristic

Shunt regulators are used at low power. To Grit the heat dissipated through the regulator.

PROBLEM ILOAD & JAPP

1

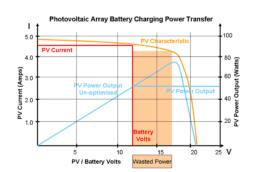
## SWITCHED MODE REGULATORS

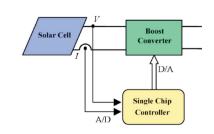
- · An electronic controller is used to decouple the solar array current from the load current.
- · Both solar array AND load can work at their optimum ament level.
- · Used to manage high power levels (>1hu)
- · Ugh esticiency but high cost and lower reliability

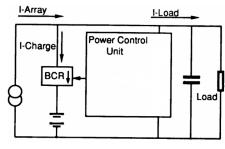
# BATTERIES APPLICATION -

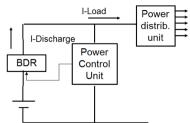
- BATTERY CHARGE REGULATOR: adjust the voltage provided by the power source to the optimum point for buttery charges.

  Remain power goes to the local.
- · BATTERY DISCUARGE REGULATOR: ensures constant voltage to the load while discharge.
- · Longer life of battery and loads at a higher cost and decrease in esticiency.





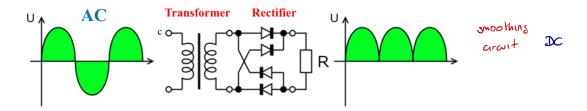




## POWER CONVERSION AND DISTRIBUTION:

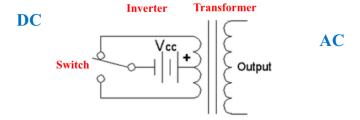
### CONVERSION: AC to DC

- · A transformer Rectifier Unit
  - 1. Trasformer reduces the AC peach voltage
  - 2. Rectifier forces the voltage to be always in the same direction
  - 3. A smothing around males the voltage constant.



## CONVERSION: DC to AC:

- · Inucrer:
  - · 3 way switches are switched back and forth with the required frequency to change the direction of the DC whent also transistors can be used.
  - · Peah voltage ca be modfied with a transformer.

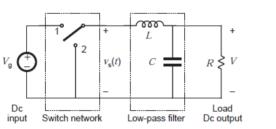


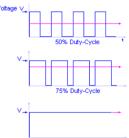
## CONVERSION: DC 60 DC

. Pulse width modulator: charges voltage.

Switch network converts the DC input into a square wave. Time % when o voltage.

A low-pass filter converts the square wave into a DC output (higher duty cycle)





CONVERSION: AC to AC

Transformer: same frequency, different peak voltage.

If we want to change frequency. AC-DC-AC conversion required.

Transformer rectifies unit + Dulse width modulator + Inverter.

Transformer

AC

IRON CORE

OUTPUT

LOAD

PRIMARY
COIL

Same frequency
Different voltage

## SIZING FOR ELECTRICAL WIRING

- · Define the length and diameter of all wires.
- · It should heep the wire loss lower than 5% in the complete circuit.
- · Wire gowse: measure of dameter of a wire
  - dower DUG -> higher diameter higher mass lower resistance
  - light wire current higher diameter -> higher mass lower AUG.

# ROCUET PROPULSION

Rochets work with the principle of action reaction, a mass is propelled in the oposite direction of motion.

- 1. The energy of the fluid is increased.
- External fluid -> aircraft internal fluid -> rochet ergne.
- 2. The energy is converted into hinetic energy.

### POSITIVES:

· Almost Independent of ambient conditions and flight velocity.

### NEGATIVES:

· Migher propellant consumption.

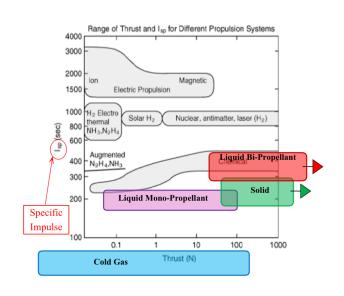
### COMPONENTS AND FUNCTIONS

- 1. Provide the fluid to be expelled (Propellant)
- 2. Store he propellant (tanks)
- 3. Feed and distribute the propellat (pipes, values...) ~ Power plant.
- 4. Accelerate the propellant (thruster)
- 5. Provide the required power to the system components. (power plant.)

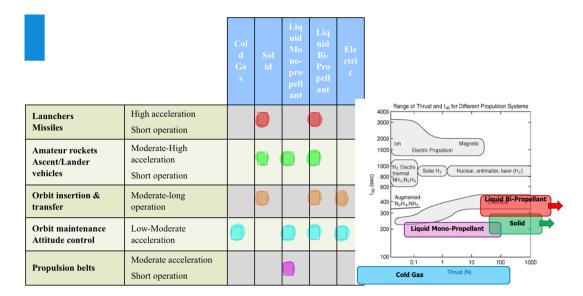
### CLASSIPICATION:

Based on: how the propellant is accelerated Thermal expansion, electrostatic forces, electromagnetic forces.

Based on: what type of energy source is used Cold gas, Chemical energy, Nuclear energy, Solar energy, Electric energy.



### APPLICATIONS:



#### PRINCIPLE WORMNG

#### MOMENTUM:

 $\vec{\perp} = M \cdot \vec{V}$ 

the momentum changes when a force acts on the body remains Constant if no force applies.

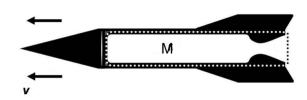
TOTAL MOLENTUM:

Sum of momentums of the different bodies in the system.

System: Mi V = MiV2

The faster we specket propellent the more relocaty we can attann.

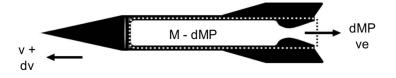
#### THE ROCKET EQUATION:



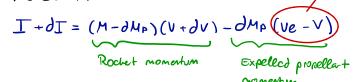
nomentum at time t:

 $T = M \cdot V$  . , no extend forces.

PROPELLANT IS EXPELLED: dMp with a jet velocity Ve: Ve is in the oposite direction to te flight direction.



MOMENTUM:



absolute velocity

a of propellant.

MULTIPLY OUT

It dI = Mu + M. dv - OMp. v - OMp. dv + OMp. v - OMp. ve Slow orher. Mu dI = M. dv - OMp. v - OMp. dv) + dMp. v - dnp. ve

dI = M. dV - drp. Ve - NO extend forces. (dI = 0) M.dV = dMp. Ve

# · separate variables and integrate

$$MdV = dMp.Ve \longrightarrow \frac{dv}{Ve} = \frac{dMp}{M} = -\frac{dM}{M}$$

$$\frac{1}{Ve} \int dV = -\int \frac{dM}{M} \longrightarrow \frac{1}{Ve} \Delta V = \ln\left(\frac{Min}{Mgin}\right)$$

## Tsiolhoushy Equation

$$\Delta V = Ve \cdot ln \left( \frac{M_{in}}{M_{in} - Mp} \right)$$

- · we have assumed Ve = constant -> NOT VALID TF
- · dMp = dM
- ' Min = initial mass of the rocket, MAn = final mass of the rocket
- · Mp total mass of propellant expelled. Mp = Min Mfn.
- · No growity
- · No oras
- · No forces
- · propellat expelled starth

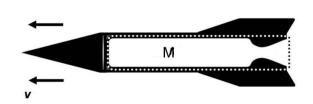
Indicator of ammount of energy needed, even if some assumptions are not tive.

### ASSUME GRAVITY FORCE

$$\Delta V = Ve \cdot ln \left( \frac{Min}{Min - Mp} \right) - g \cdot tb$$
 $g = acceleration of gravity.$ 

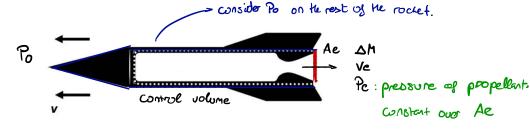
gravity loss

# KOCKET THRUST EQUATION



Before dI= M.dV - dMp. Ve -> dwide by dt

Fip is generated by the pressure of the fluid around he rocket.



FP = 
$$\int_{A_0}^{(\rho_0 - \rho_a)} dA_0 + (\rho_e - \rho_a) \cdot Ae = \overline{toras} + (\rho_e - \rho_a) \cdot Ae$$

Aerodynamic

dras. Fores

CONTROL VOLUME

For = 
$$\int_{A_0}^{A_0} P_0 \cdot dA_0 + P_0 \cdot Ae$$
 (1)

when a uniform pressure

acts on a closed surface

the total pressure force

Shall be zero.

$$\int_{A_0} \rho_a \cdot dA_0 + \rho_a \cdot Ae = 0$$
 (2)

# ROCHET THEUST EQUATION (CNTD)

$$\frac{dI}{dt} = M \cdot \frac{dV}{dt} - Ve \cdot \frac{dNp}{dt} = Fp + Foties = Foras + Foties + (Pe - Pa) \cdot Ae$$

Ropellant mass flow.

this must be also a force. - FT: rocket thinst.

$$F_T = \dot{m} \cdot Ve + (\rho e - \rho_a) \cdot Ae$$

action

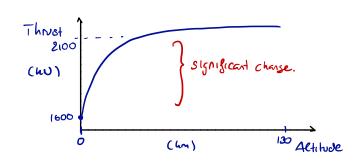
reaction

Ressure.

# ROCKET THEUST US ACTITUDE

Important to specify altitude.

- · Sea level: Pa= 101325 Pa
- Vacuum pa = 0 Pa



## LQUIVALENT DET VELOCITY

$$Veg = \frac{F_T}{\dot{m}} = Ve + \frac{(pe - pa) \cdot Ae}{\dot{m}}$$

No physical meaning, used to simplify. When W = Veg, Re = Ra  $\rightarrow \Delta V = Veg \cdot la \left( \frac{H_{in}}{H_{in} - H_{in}} \right)$ 

$$\Delta V = Veg \cdot ln \left( \frac{n_{in}}{m_{in} - n_{p}} \right)$$

# TOTAL IMPULSE

When a force acts on a body for a longer time a larger momentum change is obtained. To tale this effect into account, define total impulse.

$$Ttot = \int_{0}^{t_{b}} \frac{t_{b}}{Ft \cdot dt} \frac{Ft}{Ft \cdot dt} = \int_{0}^{t_{b}} \frac{t_{b}}{rt} \frac{Veq}{rt} = \int_{0}^{t_{b}} \frac{t_{b}}{rt} \frac{Veq}{rt} \frac{\int_{0}^{t_{b}} \frac{t_{b}}{rt}}{\int_{0}^{t_{b}} \frac{t_{b}}{rt}} \frac{Veq}{rt} \frac{\int_{0}^{t_{b}} \frac{t_{b}}{rt}}{\int_{0}^{t_{b}} \frac{t_{b}}{rt}} \frac{t_{b}}{rt}} \frac{\int_{0}^{t_{b}} \frac{t_{b}}{rt}} \frac{t_{b}}{rt}}{\int_{0}^{t_{b}} \frac{t_{b}}{rt}} \frac{t_{b}}{rt}}$$

# Specific Impulse

troportional to the total impulse divided by the total mass of propellant used

# Specific Impulse: (CNTD)

· A higher specific impulse means that a larger momentum change can be generated by a Smaller mass of propellant.

 $Tsp = \frac{Vc_s}{90} \quad . \quad \text{Specific impulse is proportional to the equivalent jet velocity.}$   $. \quad \text{Velocity change} \quad \Delta V \text{ and sochet thinst FT are also proportional }$ 

- Migner Isp = Ugner F and Myner DV Isp moreages when altitude moreages.
- go is in Isp because expresses Isp as the which is a universal measure.

# VOLUMETRIC SPECIFIC IMPULSE

Propellat volunc is used instead of propellat mass.

$$T_{\rho} = \frac{1}{g_{0}} \cdot \frac{\int_{0}^{c_{0}} F_{1} \cdot dt}{\int_{0}^{c_{0}} \frac{\dot{n}}{\rho} \cdot dt}$$
• Higher  $T_{\rho}$ : larger momentum with less volume.
• Important to define size of a rocket.

# JET POWER AND CYCLE EFFICIENCY

'Hiet: measure of available amount of power in the jet of expelled propellant

Piet = 
$$\frac{1}{2}$$
 Fr.  $\text{Veg} = \frac{1}{2} \dot{m} \cdot \text{Veg}^2$ 

Provided by the energy source - compare to Act

# HRUST POWER AND PROPULSIVE EFFICIENCY

It: measure of the ammount of power effectively used to propel the racket

Absolute jet Power: amount of jet Power not effectively used for thrust.

Pret-abs = 
$$\frac{1}{2} \dot{m} (v_{eq} - v_0)^2$$

jetabolike veloatj.

Propoles we efficiency: 
$$N_{p} = \frac{P_{T}}{P_{T} + P_{DET\_ADS}} = \frac{2 \frac{V_{o}}{V_{eq}}}{1 + (\frac{V_{o}}{V_{eq}})^{2}}$$
  
In roclets  $V_{o} > V_{eq}$  is possible 80  $V_{o} = V_{eq}$  is the optimal.

# IDEAL ROCKET THEORY:

### AUD BUILDING BLOCKS

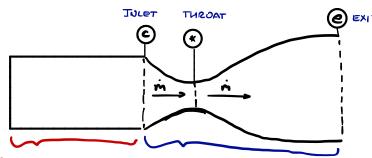
$$F_T = \dot{m} \cdot Ve - (Pe - Pa) Ae$$

$$Veg = (Ve) + \frac{(Pa - Pe) Ae}{(m)}$$

$$F_T = rin \cdot Ve - (Pe - Pa) Ae$$
  $\Delta V = Veg \cdot ln \left( \frac{Min}{Min - Mp} \right)$  depend on propellant  $Veg = Veg + \frac{(Pe) - Pa) Ae}{(rin)}$   $Tsp = \frac{Veg}{50}$   $Process$ .

heatins and acceleration process.

EVALUATION OF PARAMETERS: Ve, Pe,



EXPANSION RATIO

 $\mathcal{E} = \frac{A_{\mathbf{c}}}{A^{\mathbf{x}}}$ 

Combustion chambe

Convergent - Divergent Noorle

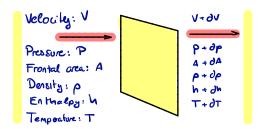
- · Uigh preasure
- · (Uigh temperature)
- · Low speed
- · Propellant is accelerated
- · No external energy is provided.

### ASSUMPTIONS:

- 1.) Propellant in the chamber + norther is a perfect gas.
- 2.) Propellant in the chamber + norther is a callonically ideal gas (specific heats are not dependent on temperature).
- 3.) Propellant in the chamber + norther has homogeneous and constant chemical composition.
- 4.) Flow in the nortle is steady (not dependent on time)
- 5.) Flow in the notale is isentropic (no external energy applied, no lost)
- 6.) Flow in the notate is 1.-dimensional (quantities vary along notate axis)
- 7.) Flow velocty is purely amal.
- 8.) No external forces act on the propellant flowing in the notate.
- 9.) Propellant in the chamber has negligible viclosity. (10 0)

### CONSERVATION EQUATIONS:

Mass, momentum and energy: variohous are very small, because we are considerns a small nottle portion.



## MASS CONSERVATION EQUATION:

$$\dot{m} = \rho \cdot V \cdot A$$
 no mass generated or extracted  $\longrightarrow \frac{d(\rho V \cdot A) = 0}{\rho V A} = constant$ 

## MOMENTUM CONSERVATION EQUATION:

$$d(\dot{m} \cdot V) = p \cdot A - (p + dp) \cdot A \longrightarrow \dot{m} \cdot dv = -A \cdot dp$$

$$\dot{m} = \rho \cdot v \cdot A \longrightarrow \dot{m} \cdot dv = \rho \cdot v \cdot A \cdot dv = -A \cdot d\rho$$

$$dP + \rho \cdot v \cdot dv = 0$$

$$P + \frac{1}{2}\rho v^2 = cons tant$$

# ENERGY CONSERVATION EQUATION

The propellant does not exchange any energy, no total enthalpy variations are possible:

$$d\left(h + \frac{1}{2}v^2\right) = 0$$

$$d\left(h + \frac{1}{2}V^2\right) = 0$$

$$dh + VdV = 0$$

$$Jwte624710N$$

$$h + \frac{1}{2}V^2 = constant$$

# TOEAL GAS EQUATIONS

### EQUATION OF STATE

- ρ: gas density

- . T: gas Temperature
- · Mu :gas molecular mass
- · RA: universal sas constant 8314 ]/(kexhanol)

$$Y = \frac{C_p}{C_v}$$

$$\frac{R_A}{M\omega} = C\rho - Cv$$

$$Y = \frac{C_D}{C_V}$$

$$C_D = \frac{\gamma}{\gamma - 1} \cdot \frac{R_A}{M\omega}$$

- · Cp: constart pressue specific heat
- · Cu: constant volume specific heat.

### ISENTROPIC FLOW:

$$\frac{P}{P^6} = constant$$

$$\frac{P}{P^{\delta}} = constant$$
  $P \cdot T \left(\frac{V}{4-V}\right) = constant$ 

#### MACH NUMBER

$$M = \frac{V}{a}$$
  $a^2 = \left(\frac{\partial P}{\partial \rho}\right)_{constant}$  entropy

$$a^2 = \gamma \cdot \frac{R_0}{H_W} \cdot T = \gamma \cdot \frac{P}{P}$$

# CONVERGENT - DIVERGENT NOTTLE:

Differentiating the mass conservation equation and dividing by the (constant) mass flow rate:

$$\partial(\rho \cdot V \cdot A) = 0 \longrightarrow \frac{\partial V \cdot \partial A}{\rho \cdot N \cdot A} + \frac{V A \cdot \partial \rho}{\rho \cdot N \cdot A} + \frac{\partial A \cdot \partial V}{\rho \cdot N \cdot A} = 0 \qquad \frac{\partial A}{\partial A} + \frac{\partial \rho}{\partial A} + \frac{\partial V}{\partial V} = 0$$

Momentum conservation equation and speed of sound:

$$\frac{d\rho + \rho \vee d\nu = 0}{\rho} = -\frac{d\rho}{d\rho} \cdot \vee \cdot d\nu = -\frac{V^2}{\alpha^2} \cdot \frac{d\nu}{\nu} = -\frac{d\nu}{\Delta} \cdot \frac{d\nu}{\nu}$$

$$\frac{d\rho}{\partial \rho} = -\frac{d\rho}{d\rho} \cdot \vee \cdot d\nu = -\frac{V^2}{\alpha^2} \cdot \frac{d\nu}{\nu} = -\frac{d\nu}{\Delta} \cdot \frac{d\nu}{\nu}$$

$$\frac{dA}{A} = (M^2 - 1) \frac{d\nu}{\nu}$$

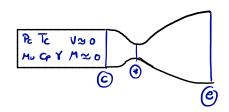
	M < 1	M > 1	`			
CONVERGENT   dA < C	dv>0	du c0		· Convergent when M < 1 · Divergent when M > 1	When $M=1$ $dA=0$	)
DIVERSENT DA >0	du<0	du>0	1	2,003,000	throat	throat

THE NOTICE SUOULD BE DESIMED TO MANE M=1 AT NOTICE

## NOTTLE FLOW EQUATIONS

#### **LUUITAMUSZA**

Conditions of propellant in the chamber are known. To, Pc propellant composition and characteristics are known. Y, Cp, Mw -s constant.



ENERGY EQUATION:

$$h + \frac{1}{2}V^2 = constant$$

$$h = Cp \cdot T$$

$$Cp Tc + O = Cp \cdot T + \frac{1}{2}V^2$$

$$Chamber$$

$$Generic norde.$$

REDUCTE AS: > SPECIFIC MEAT AND ISENTED PIC TELOW

$$V = \sqrt{2C\rho \cdot (T_{C} - T)}$$

$$C\rho = \frac{\gamma}{\gamma_{-1}} \cdot \frac{R_{A}}{M_{W}} \longrightarrow V = \sqrt{\frac{2\gamma}{\gamma_{-4}} \cdot \frac{R_{A}}{M_{W}} \cdot (T_{C} - T)} = \sqrt{\frac{2\gamma}{\gamma_{-1}} \cdot \frac{R_{A}}{M_{W}} \cdot T_{C} \cdot \left(1 - \frac{T}{T_{C}}\right)}$$

$$= \sqrt{\frac{\gamma_{-1}}{\gamma_{-1}} \cdot \frac{R_{A}}{M_{W}} \cdot T_{C} \cdot \left(1 - \frac{T}{T_{C}}\right)}$$

$$PT \left( \frac{\delta}{1-\delta} \right) = Constant \qquad \frac{T}{T_{c}} = \left( \frac{P}{P_{c}} \right) \frac{\gamma - 1}{\delta}$$

$$V = \sqrt{\frac{2\gamma}{\gamma - 1} \cdot \frac{R_{A}}{M_{W}} \cdot T_{c}} \left[ 1 - \left( \frac{P}{P_{c}} \right) \frac{\gamma - 1}{\delta} \right]$$

$$V_e = \sqrt{\frac{2Y}{Y-1} \cdot \frac{R_A}{M_W} \cdot T_C} \left[ 1 - \left( \frac{R_e}{R_c} \right)^{\frac{Y-1}{Y}} \right]$$

VIEWER DET VELOCITY:

- · Increasing To
- · Reducing Exit pressure
- · Reducing Mw

 $Ve\_limit$  is attained when the exit pressure Pe=0.

MASS FLOW RATE AND EXPANSION RATIO

MACH NUMBER RELATIONS:

$$C_{p}T_{c} = C_{p}T + \frac{1}{2}v^{2} \longrightarrow \frac{T_{c}}{T} = 1 + \frac{v^{2}}{2C_{p}T}$$

$$P + \left(\frac{3}{4-1}\right) = constant$$

$$C\rho = \frac{\gamma}{\gamma - 1} \cdot \frac{\Omega_A}{M_w}$$

$$C\rho T = \frac{1}{\gamma - 1} \cdot \left( \frac{\Omega_A}{M_w} \cdot T \right) = \frac{\Omega^2}{\gamma - 1}$$

$$\frac{T_c}{T} = 1 + \frac{\gamma - 1}{2} \cdot \frac{V^2}{\alpha^2} = 1 + \frac{\gamma - 1}{2} \cdot M^2$$

SONIC THEOAT

$$\frac{T_{c}}{T_{x}} = 1 + \frac{Y-1}{2} = \frac{1+Y}{2}$$

$$\frac{P_{c}}{P^{x}} = \left(\frac{1+Y}{2}\right)^{\frac{\gamma}{\gamma-1}}$$

$$\frac{P_c}{P^*} = \left(\frac{1+Y}{2}\right)^{\frac{\gamma}{\gamma-1}}$$

MASS FLOW RATE EQUATIONS

• 
$$\frac{\dot{m}}{A} = \rho \cdot V = \rho_c \cdot \frac{\rho}{\rho_c} \cdot \sqrt{\frac{2 \, \gamma}{3-1} \cdot \frac{R_A}{M_W} \cdot T_C \left[1 - \left(\frac{P}{P_c}\right)^{\frac{\gamma-1}{\gamma}}\right]}$$

• 
$$\frac{\dot{M}}{A} = \rho \cdot V = \rho_{c}$$
.  $\frac{R_{A}}{M_{w}} \cdot T_{c} \cdot \sqrt{\frac{2 r}{r-1}} \cdot \left(\frac{P}{P_{c}}\right)^{2} \left[1 - \left(\frac{P}{P_{c}}\right)^{\frac{\gamma-1}{\gamma}}\right]$ 

$$\frac{\dot{M}}{A} = \frac{P_{c}}{\left(\frac{P_{c}}{M_{\omega}} \cdot T_{c}\right)} \cdot \sqrt{\frac{2\gamma}{\gamma_{-1}} \left(\frac{P}{P_{c}}\right)^{\frac{2}{\gamma}} \cdot \left[1 - \left(\frac{P}{P_{c}}\right)^{\frac{\gamma-1}{\gamma}}\right]}$$

$$P_c = \rho_c \cdot \frac{R_A}{M_W} T_c$$

$$\rho_c = \frac{P_c}{\frac{R_A}{M_W} T_c}$$

SONIC TUROAT

$$\frac{P_c}{P^*} = \left(\frac{1+8}{2}\right)^{\frac{\gamma}{3-1}} \longrightarrow \frac{P^*}{P_c} = \left(\frac{1+\gamma}{2}\right)^{\frac{\gamma}{1-\gamma}}$$

$$\frac{\dot{M}}{A^{4}} = \frac{P_{c}}{\left(\frac{P_{c}}{A} \cdot T_{c}}\right) \cdot \sqrt{\frac{2^{3}}{\gamma_{-1}} \left(\frac{P^{*}}{P_{c}}\right)^{\frac{2}{\gamma}}} \cdot \left[1 - \left(\frac{P^{*}}{P_{c}}\right)^{\frac{3-1}{\gamma}}\right] = \frac{P_{c}}{\sqrt{\frac{P_{c}}{M_{c}} \cdot T_{c}}} \cdot \sqrt{\frac{2^{3}}{\gamma_{-1}} \cdot \left(\frac{A+Y}{2}\right)^{\frac{2}{A+3}}} \cdot \left[A - \left(\frac{A+Y}{2}\right)^{\frac{2}{A+3}}\right]$$

$$\dot{M} = \frac{P_{c} \cdot A^{*}}{\sqrt{\frac{R_{a}}{H_{w}} \cdot T_{c}}} \cdot \Gamma(\gamma) = \sqrt{\gamma \cdot \left(\frac{1+\gamma}{2}\right)^{\frac{1+\gamma}{4-\gamma}}} \quad \begin{cases} \text{Vanden herch hove} \\ \text{Functions} \end{cases}$$

only one value males the throat conditions possible (chocked flow)

## AREA RATIO EQUATION

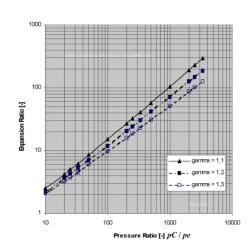
$$\frac{A}{A^*} = \frac{\Gamma(\Upsilon)}{\sqrt{\frac{2\Upsilon}{\Upsilon-1} \cdot \left(\frac{\rho}{\rho_c}\right)^{2/\Upsilon} \cdot \left[\Lambda - \left(\frac{\rho}{\rho_c}\right)^{\frac{\Upsilon-1}{2}}\right]}}$$

- · for a siven chamber conditions (pc , T) and throat area A\*, this equation gives the flow pressure corresponding to each notitle section of area A.
  - · Two solutions for each erea, subsonic, supersonic.

EXIT AREA RATIO:

$$\mathcal{E} = \frac{Ae}{A^*} = \frac{\Gamma(\Upsilon)}{\sqrt{\frac{2\Upsilon}{\gamma-1} \cdot \left(\frac{P_e}{P_c}\right)^{2/\gamma} \cdot \left[1 - \left(\frac{P_e}{P_c}\right)^{\frac{\gamma-1}{\gamma}}\right]}}$$
The pressure ratio Pe/Pc can be calculated as a further of  $\chi$  and  $\chi$ 

- · Direct relationship between expansion
- calculated as a function of & and (Ae, A\*)

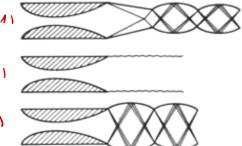


### EXPAUSION CONDITIONS:

11) Pe < Pa our expended

(2) Pe = Pa adapted expanded (2)

(3) Pe > Pa under-expanded



(1), (3) Shoch wares are oreated to adapt to Pa.

## CHARACTERISTIC VELOCITY AND THRUST COEFFICIENT

TURUST EQUATION:

COMBINING THE PREVIOUS GRUATIONS

$$F_{T} = p_{C} \cdot A^{*} \cdot \Gamma \left( \gamma \right) \cdot \sqrt{\frac{2\gamma}{\gamma - 1} \cdot \left[ 1 - \left( \frac{p_{e}}{p_{C}} \right)^{\frac{\gamma - 1}{\gamma}} \right]} + \left( p_{e} - p_{a} \right) \cdot \frac{A^{*} \cdot \Gamma \left( \gamma \right)}{\sqrt{\frac{2\gamma}{\gamma - 1} \cdot \left( \frac{p_{e}}{p_{C}} \right)^{\frac{2}{\gamma}} \cdot \left[ 1 - \left( \frac{p_{e}}{p_{C}} \right)^{\frac{\gamma - 1}{\gamma}}} \right]}$$

- · FIXED NOTTLE GEOMETRY MAXIMUM THRUST WHEN (Pa = 0)
- · FIXED ATMOSPHERIC PRESSURE MAXIMUM THRUST (Pa = Pe)

CHARACTERISTIC VELOCITY:

$$C^* = \frac{P_{c} \cdot A^*}{r^{i}}$$

TURUST COEFFICIENT:

$$C^* = \frac{P_{C \cdot A^*}}{P_{C \cdot A^*}}$$

$$C_F = \frac{F_T}{P_{C \cdot A^*}}$$

$$C_F = \frac{F_T}{P_{C \cdot A^*}}$$

$$C_{F \cdot A^*}$$

$$C_{F \cdot$$

CHARCACTERISTIC VELOCITY

$$C^* = \frac{1}{\Gamma(\gamma)} \cdot \sqrt{\frac{\Re_A}{\pi_{\omega}} \cdot T_c}$$

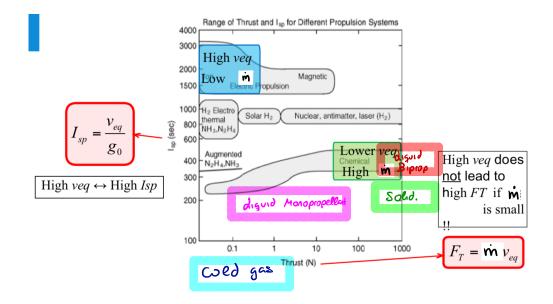
 $C^{\times} = \frac{1}{\Gamma(\gamma)} \cdot \sqrt{\frac{R_A}{M_W}} \cdot T_C$  Depends only of measur performance of propellant. Better.

THOUST COEFFICIENT

$$C_{F} = \frac{F_{T}}{p_{C} \cdot A^{*}} = \Gamma\left(\gamma\right) \cdot \sqrt{\frac{2\gamma}{\gamma - 1}} \cdot \left[1 - \left(\frac{p_{e}}{p_{C}}\right)^{\frac{\gamma - 1}{\gamma}}\right] + \left(\frac{p_{e}}{p_{C}} - \frac{p_{a}}{p_{C}}\right) \cdot \frac{\Gamma\left(\gamma\right)}{\sqrt{\frac{2\gamma}{\gamma - 1}} \cdot \left(\frac{p_{e}}{p_{C}}\right)^{\frac{2}{\gamma}} \cdot \left[1 - \left(\frac{p_{e}}{p_{C}}\right)^{\frac{\gamma - 1}{\gamma}}\right]}}$$
Depends mainly on notifle geometry. (Pe/Pe)

measure of effects on norre geometry.

## CLASSIFICATION OF ROCHET ENGINES



# COLD GAS ROCHETS: Attitude control.

- · Not heated, accelerated from the chamber at ambient temperature.
- · Thrust from propellant pressurization
  PERFORMANCE

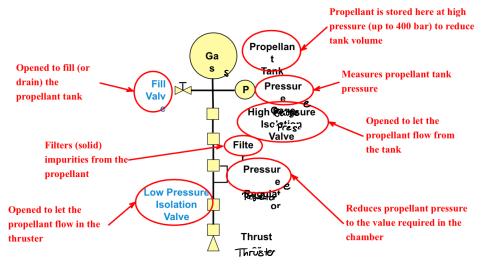
dow Isp, dow Thrust.

#### DISADVANTAGES

To low, limited performance (jet velocity and specific impulse)

AD VANTAGES

Simplicity and safety.



· Compact, small satellites.

### PROPELLANTS

- · Gaseous at ambient conditions
- · Chemically net, safe Wellow and Nitrogen.
- . dowest Mu generate Vishest Isp (Melium)
- · Uistest Mw senerate Vistest Ip (xenon) dess volume used.

## BUW-DOWN SYSTEMS

No pressure regulator is used Pt = Pc
15 to 30 bar = Pt

Tanh pressure Pt decreases with time

$$\frac{P_{T}}{P_{T}}$$
 = constant

· Isetropic: h= 8

\*Isothermal: h= 1

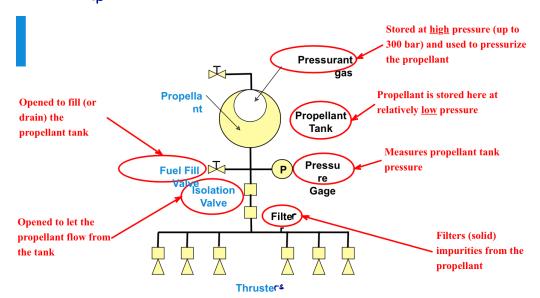
 $\frac{P_{t}}{M_{T}}$  = constant

LIQUID MONO-PROPELLANT ROCKETS attitude controls, propulsion belts

- · Propellants are heated by a chemical reaction in the combustion Chamber.
- . Energy used to severate thoust comes from propellant pressurgation and from cherrical reaction.
- · The chemical reaction is a decomposition of the propellant.

### PERFORMANCE

Low Isp (200) don Thrust (2011)



### PEOPELLAUTS:

- · Nydrazine
- · Mydroson peroxide

## CHAMBER TEMPERATURE

• The decomposition power Pdec of a mono propellant can be expressed as a function of:

- · Power needed to increase the temperature of decomposition products from to to To is:

  Theat = M·Cp·(Tc-To)
- Assume that Polec is used to heat the products of the decomposition

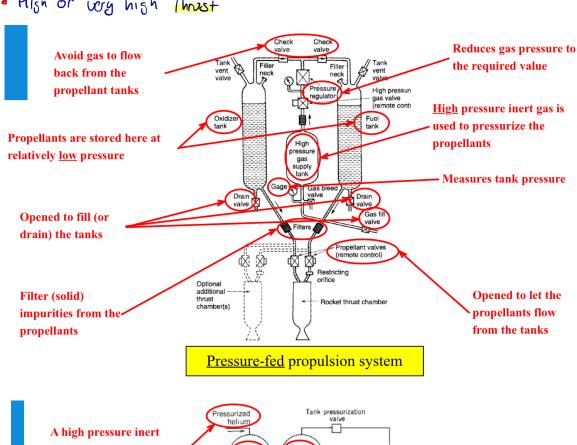
  Pheat = Polec → M·No = M·Cp·(Tc-To) → Tc = To + No
  Cp

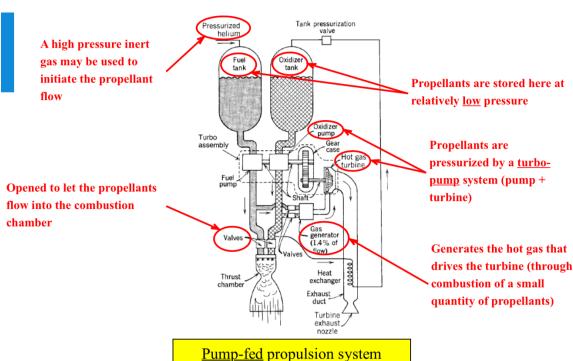
LIQUID BI - PROPELLANT ROCHETS danchers, missiles, orbit insertion, transfer orbits.

- · Two Propellants are used (oxidizer and fuel) combustion
- · Mypergalic propellants if combustion takes place spontaneously when they enter in contact.
- · Oxdizer/fuel ratio (O/F) is the ratio of oxidizer to fuel mass flow rates:

## PERFORMANCE

- · Relatively high Isp
- · Hish or very high Thrust





# PROPELLANTS

- · Oxidizes: Liquid Oxigen, Nitrogen Tetroxide, Midrogen Peroxide, Nitrous Oxide
- · FUELS: diquid Vidroson, diquid Methane, herosene, Mydrozine

ROCKET PROPELLANT PERFORMANCE  Combustion chamber pressure, $P_e = 68$ atm (1000 PSI) Nozzle exit pressure, $P_e = 1$ atm								
Liquid Oxygen teap.  Very low to heep hen	Liquid Hydrogen	No	5.00	381 n. 2	124			
	Liquid Methane	No	2.77	299	235			
	Ethanol + 25% water	No	1.29	269	264			
	Kerosene	No	2.29	289	294			
	Hydrazine	No	0.74	303	321			
	ММН	No	1.15	300	298			
	UDMH	No	1.38	297	286			
	50-50	No	1.06	300	300			
Liquid Fluorine	Liquid Hydrogen	Yes	6.00	(400) n. 1	155			
	Hydrazine	Yes	1.82	338	432			
FLOX-70	Kerosene	Yes	3.80	320	385			
Nitrogen Tetroxide	Kerosene	No	3.53	267	330			
	Hydrazine	Yes	1.08	286	342			
	ммн	Yes	1.73	280	325			
	UDMH	Yes	2.10	277	316			
	50-50	Yes	1.59	280	326			
Hydrogen Peroxide	Kerosene	No	7.84	258	324			
(85% concentration)	Hydrazine	Yes	2.15	269	328			
Nitrous Oxide	HTPB (solid)	No	6.48	248	290			
Chlorine Pentafluoride	Hydrazine	Yes	2.12	297	439			
Ammonium Perchlorate (solid)	Aluminum + HTPB (a)	No	2.12	266	469			
	Aluminum + PBAN (b)	No	2.33	267	472			
Red-Fuming Nitric Acid (14% N <sub>2</sub> O <sub>4</sub> )	Kerosene	No	4.42	256	335			
	Hydrazine	Yes	1.28	276	341			
	ММН	Yes	2.13	269	328			
	UDMH	Yes	2.60	266	321			
	50-50	Yes	1.94	270	329			

## EMPERATURE

Combustion Power Promb can be expressed as:

Promb = influer. No - Meating value of fuel at latin and 298 K

Power Pheat needed to increase the temperature of combustion products from their initial value To to a final value To must take into account the entire amount of propellant (Firel + 0 xid)

Equating fromb and Pheat we get the chamber temporatue

# COMBUSTION PRODUCTS PROPERTIES

The combustion products properties are evaluated as molar average of the properties of the single components.

$$N_{CO2} = 12 \text{ notes}$$
 3 molar averaged values of Gp and Mw  $N_{H2O} = 13$   $C_{ID} = \frac{12 \cdot C_{ID} \cdot C_{ID}}{12 + 13}$ 

MW = same

# PUMP-FED ROCLETS

darge ensures, not combinient to use pressure gas (too heavy).

Propellants are pressurized by a pump.

More convinient when tunst is higher than 20 ho

Power reguled by the pump:

Poump = 
$$\frac{\dot{M} \cdot \Delta \rho}{V \cdot \rho}$$
 Regulared pressure increase.

Pump egliciency (SD %)

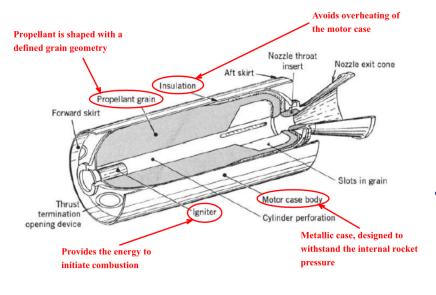
# SOLID PROPELLANT ROCLETS

Oxidizo and fuel are mixed together in a solid-state grain.

The combustion is initiated by an igniter and can not be stopped once started.

No propellant seed system is needed: simpler

Mass flow rate is much higher than liquid. More or less some Isp but higher thrust.



### REGRESSION RATE

Mass flow rate:

Regression rale:

## CHAMBER PRESSURE

mass flow rate is also

$$\dot{M} = \frac{\Re \cdot A^*}{C^*}$$

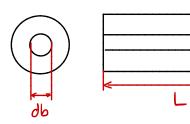
Combining the two equations:

$$\dot{m} = \rho_s \cdot a \cdot P_c^{\mu} \cdot \Delta b = \frac{P_c \cdot A^*}{c^*}$$

$$P_{c} = \left(\frac{C \cdot \rho_{8} \cdot C^{*}}{A^{*}} \cdot \Delta b\right)^{\frac{1}{A-N}}$$

- charge with time.

## GRAIN SHAPES:



 $Ab = n \cdot db \cdot L$ 

· Since diameter db increases during burning the burning surface also increases.