

Delft University of Technology
DEPARTMENT OF AEROSPACE ENGINEERING

Course: Thermodynamics and compressible aerodynamics;

Code AE2125

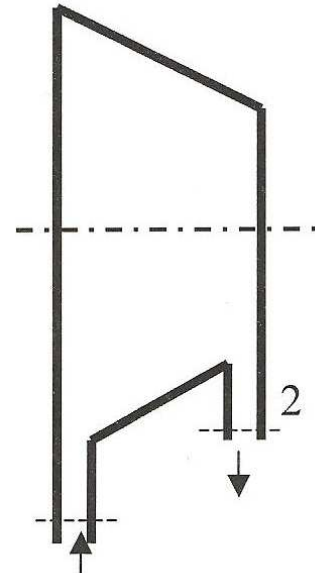
Course year: 2

Date: Thursday 8th April 2010

Time: 10:00 –12:00

Problem 1-a

Consider a thermally insulated compressor, as depicted in fig. 1. Air is compressed from ambient conditions (where air is assumed at rest) to a pressure of 400 kPa and a temperature of 480K. The speed of air at the outlet of the turbine is 100 m/s and the mass flow through the compressor is 1.5 kg/s.



1 (ambient; $T_1=25^\circ\text{C}$; $p_1=100\text{kPa}$)

Fig. 1 –compressor schematic.

Answer the following questions:

- 1) determine the power required by the compressor;
- 2) verify that the transformation followed by the gas is irreversible;
- 3) represent the transformation 1-2 in the T - s plane;
- 4) determine the power that would have been required by the compressor in case of isentropic compression from the same initial state to the same final pressure and same final speed;
- 5) calculate the isentropic efficiency of the compressor;

Problem 1-b

Consider a piston-cylinder device containing carbon dioxide at 300 KPa, 100 °C in an initial volume of 0,2 m³. The piston is slowly loaded with a series of weights in such a way that the gas is compressed until it reaches a temperature of 200 °C. The compression can be considered a polytropic transformation with exponent $n = 1.3$.

Assuming that the carbon-dioxide behaves like a perfect gas:

- 1) Determine the work exchanged during the transformation; is the gas receiving or providing work from/to the surroundings?
- 2) Determine the heat exchanged by the gas; is the gas receiving or providing heat from/to the surroundings?
- 3) Does the heat exchange increase or decrease when the gas is replaced by air? Justify your answer.

Problem 1-c

Consider a pure substance, e.g. H₂O, contained in a piston-cylinder device undergoing a change in its phase at constant pressure from the liquid to vapor phase.

- 1) Draw the schematic evolution of the transformation followed by the substance in the (T,v) thermodynamic plane as a function of the substance pressure;
- 2) Identify the position of the saturated liquid and saturated vapor states in the (T,v) plane as a function of pressure; is there a particular point where these states coincide?
- 3) Give the definition of the so called “quality of a mixture”. Derive the formula relating the quality of a mixture to the mixture specific volume and the specific volumes of the corresponding saturated liquid and vapor states at the same pressure.

Appendix : Air properties: $C_p = 1004 \text{ J/Kg K}$; $\gamma = 1.4$; Carbon dioxide properties : $C_p = 844 \text{ J/Kg K}$; $\gamma_{\text{CO}_2}=1,289$