

\*8/144  $I = \int F dt = m\dot{x}$ ,  $8 = 4\dot{x}$ ,  $\dot{x} = 2 \text{ m/s}$  at  $t \approx 0$   
 After impulse, oscillator obeys Eq. 8/9 with  $\zeta = 0.1 < 1$   
 so underdamped with solution given by Eq. 8/12

$$x = Ce^{-\zeta\omega_n t} \sin(\omega_d t + \psi), \quad C, \psi \text{ constants}$$

$$\dot{x} = -C\zeta\omega_n e^{-\zeta\omega_n t} \sin(\omega_d t + \psi) + Ce^{-\zeta\omega_n t} \omega_d \cos(\omega_d t + \psi)$$

$$\text{where } \omega_n = \sqrt{k/m} = \sqrt{200/4} = 7.07 \text{ rad/s,}$$

$$\omega_d = \omega_n \sqrt{1 - \zeta^2} = 7.07 \sqrt{1 - 0.1^2} = 7.04 \text{ rad/s}$$

$$\text{When } t = 0, x = 0, \text{ so } 0 = C \sin \psi, \quad \psi = 0$$

$$\text{" " , } \dot{x} = 2 \text{ m/s, so } 2 = -C(0.1)(7.07)(0) + C \times 7.04, \quad C = 0.284 \text{ m}$$

$$\text{Thus } \underline{x = 0.284 e^{-0.707t} \sin 7.04t}$$

